

## Bi177 - Lecture 10

### “Quantitative“ Fluorescence

Fluorescence linearity (non-linearity)

Dye, microscope, camera

Flat-fielding to linearize

Quantitating the image

Multispectral imaging

FRET

Our discussion of fluorescence has made hidden assumption that dyes have an ideal behavior

How true is this?



Fluorescent Dye

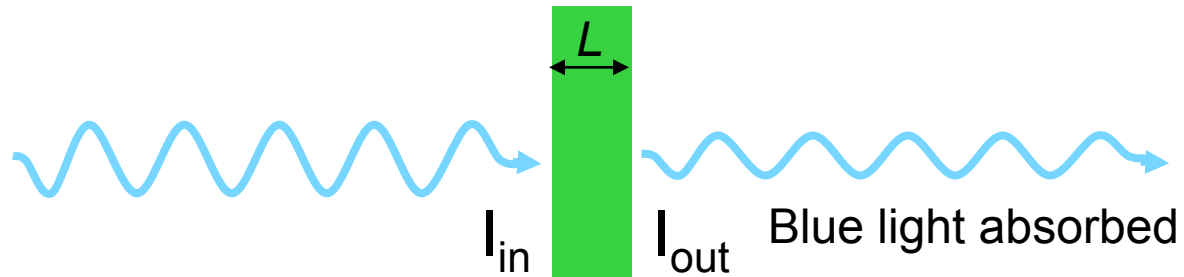
Dipole antenna

Delocalized electrons

Longer dipole, longer  $\lambda$

# Fluorophore absorption

Green dye in cuvette



Beer-Lambert law

$$I_{out} = I_{in} \exp(-\epsilon L c)$$

$$I_{absorbed} = I_{in} - I_{out}$$

$I_{in}$ : incident light intensity (in  $\text{W}\cdot\text{cm}^{-2}$ )

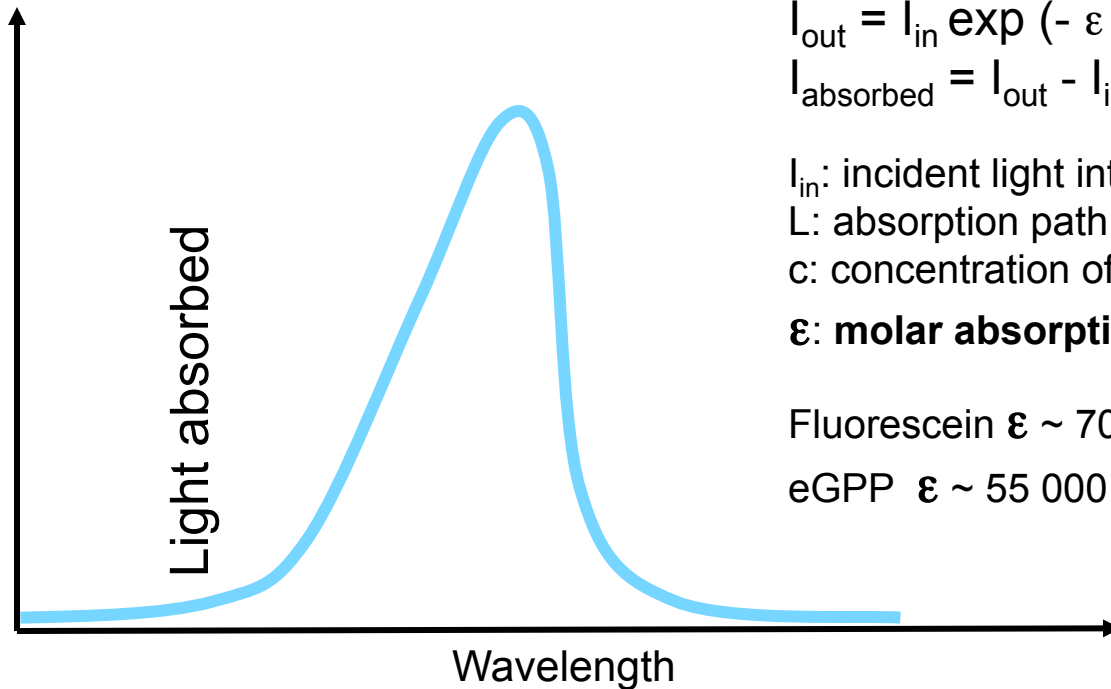
$L$ : absorption path length (in cm)

$c$ : concentration of the absorber (in M or  $\text{mol}\cdot\text{L}^{-1}$ )

$\epsilon$ : **molar absorption coefficient** (in  $\text{M}^{-1}\text{cm}^{-1}$  or  $\text{mol}^{-1}\cdot\text{L}\cdot\text{cm}^{-1}$ )

Fluorescein  $\epsilon \sim 70\,000 \text{ M}^{-1}\cdot\text{cm}^{-1}$

eGFP  $\epsilon \sim 55\,000 \text{ M}^{-1}\cdot\text{cm}^{-1}$



# Fluorophore absorption

Other expressions of the Beer-Lambert law:

$$I_{\text{out}} = I_{\text{in}} \exp(-\varepsilon L c)$$

$$I_{\text{out}} = I_{\text{in}} \exp(-\sigma L N)$$

$$I_{\text{out}} = I_{\text{in}} \exp(-\mu_a L)$$

$I_{\text{in}}$ : incident light intensity in  $\text{W}\cdot\text{cm}^{-2}$

$L$ : absorption path length in  $\text{cm}$

$c$ : concentration of the absorber in  $\text{M}$  or  $\text{mol}\cdot\text{L}^{-1}$

$N$ : density of the absorber in  $\text{molecule}\cdot\text{cm}^{-3}$

$\varepsilon$ : **molar absorption coefficient** in  $\text{M}^{-1}\text{cm}^{-1}$  or  $\text{mol}^{-1}\cdot\text{L}\cdot\text{cm}^{-1}$

$\sigma$ : **absorption cross section** in  $\text{cm}^2$  or  $\text{cm}^2\cdot\text{molecule}^{-1}$

$\mu_a$ : **absorption coefficient** in  $\text{cm}^{-1}$

$$N = N_{\text{Avogadro}} \cdot 10^{-3} c \quad (1\text{L} = 10^3 \text{cm}^3)$$

$$\varepsilon = N_{\text{Avogadro}} \cdot 10^{-3} \sigma = 6.022 \cdot 10^{20} \sigma$$

eGFP

$$\varepsilon = 55\,000 \text{ M}^{-1}\cdot\text{cm}^{-1}$$

$$\sigma = 9.13 \cdot 10^{-17} \text{ cm}^2\cdot\text{molecule}^{-1}$$

# Fluorophore absorption

## In the literature...

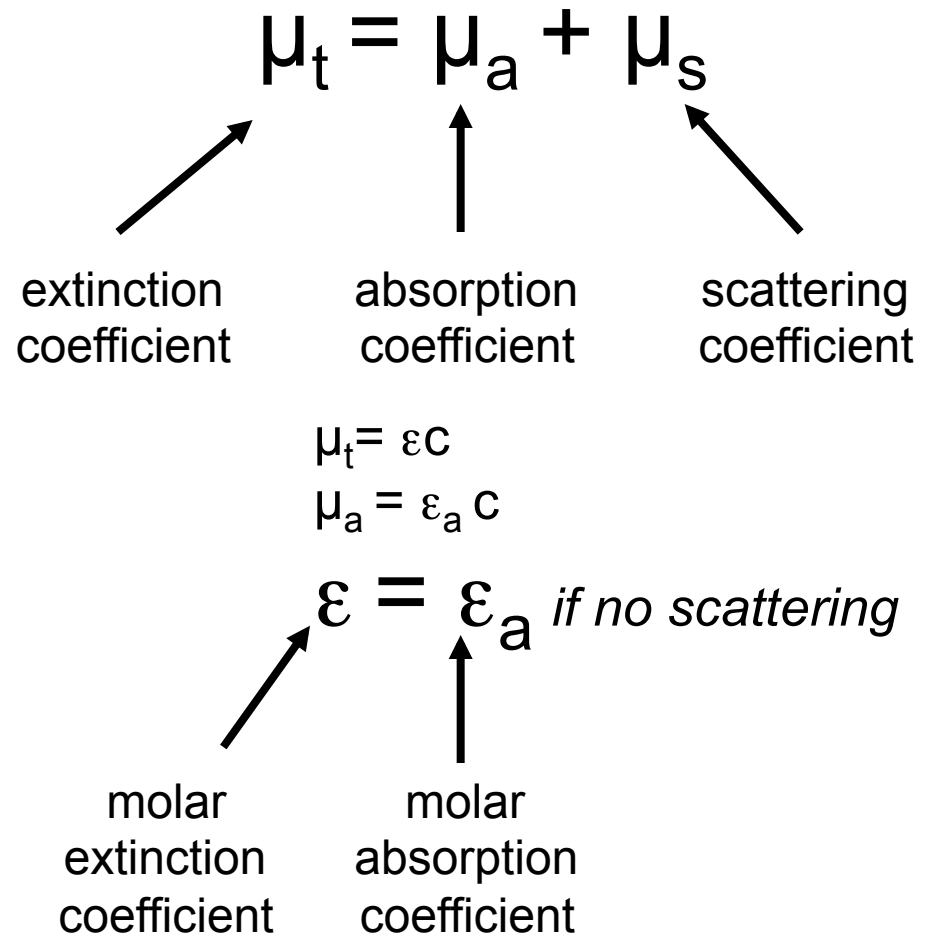
The “extinction coefficient” is usually given in tables.

confusions:

- “extinction coefficient” used for “absorption coefficient” (it assumes the scattering coefficient is negligible)
- “extinction coefficient” used for “molar extinction coefficient” (check the unit!)

$\epsilon(\lambda)$ !

The maximum is given in tables, or the excitation wavelength is indicated.



# Fluorophore absorption

Example: properties of fluorescent protein variants

Table 1 Properties of novel fluorescent protein variants *it is the molar absorption coefficient*

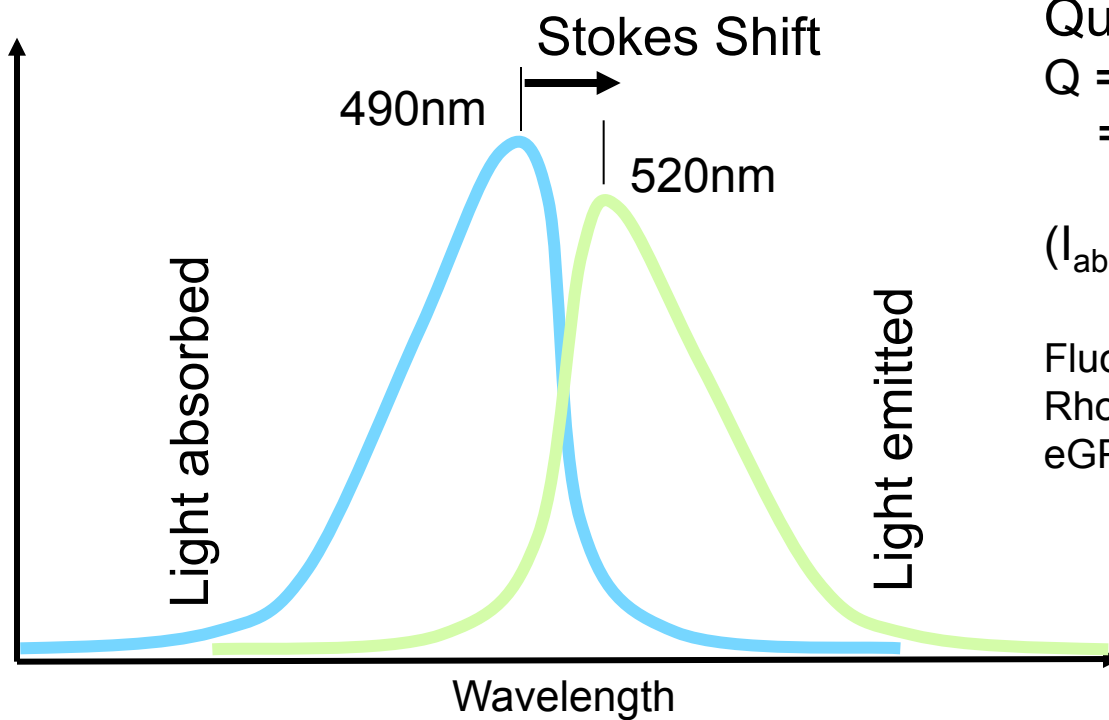
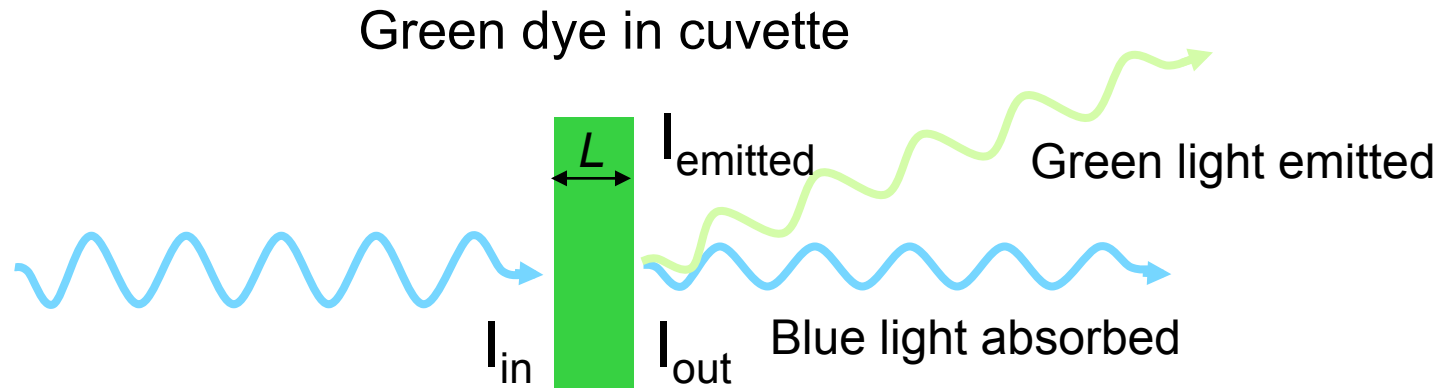
Fluorescent protein	Excitation maximum (nm)	Emission maximum (nm)	Extinction coefficient per chain <sup>a</sup> ( $M^{-1}cm^{-1}$ )	Fluorescence quantum yield	Brightness of fully mature protein (% of DsRed)	pKa	$t_{0.5}$ for maturation at 37 °C	$t_{0.5}$ for bleach <sup>b</sup> , s
DsRed	558	583	75,000	0.79	100	4.7	~10 h	ND
T1	555	584	38,000	0.51	33	4.8	<1 h	ND
Dimer2	552	579	69,000	0.69	80	4.9	~2 h	ND
mRFP1	584	607	50,000	0.25	21	4.5	<1 h	6.2
mHoneydew	487/504	537/562	17,000	0.12	3	<4.0	ND	5.9
mBanana	540	553	6,000	0.70	7	6.7	1 h	1.4
mOrange	548	562	71,000	0.69	83	6.5	2.5 h	6.4
dTomato	554	581	69,000	0.69	80	4.7	1 h	64
tdTomato	554	581	138,000	0.69	160	4.7	1 h	70
mTangerine	568	585	38,000	0.30	19	5.7	ND	5.1
mStrawberry	574	596	90,000	0.29	44	<4.5	50 min	11
mCherry	587	610	72,000	0.22	27	<4.5	15 min	68

<sup>a</sup>Extinction coefficients were measured by the alkali denaturation method<sup>8,30</sup> and are believed to be more accurate than the previously reported values for DsRed, T1, dimer2 and mRFP1<sup>7</sup>.

<sup>b</sup>Time (s) to bleach to 50% emission intensity, at an illumination level that causes each molecule to emit 1,000 photons/s initially, that is, before any bleaching has occurred. See Methods for more details. For comparison, the value for EGFP is 115 s, assuming an extinction coefficient of  $56,000 M^{-1}cm^{-1}$  and quantum efficiency of 0.60 (ref. 30). ND, not determined.

Shaner et al, Nature Biotechnology, 2004

# Fluorophore quantum yield Q



## Quantum Yield

$$Q = I_{emitted} / I_{absorbed}$$
$$= \# \text{ photons emitted} / \# \text{ photons absorbed}$$

$$(I_{absorbed} = I_{out} - I_{in})$$

Fluorescein	Q ~ 0.8
Rhodamine B	Q ~ 0.3
eGFP	Q ~ 0.6

# Fluorophore brightness = $\epsilon Q$

## Example: properties of fluorescent protein variants

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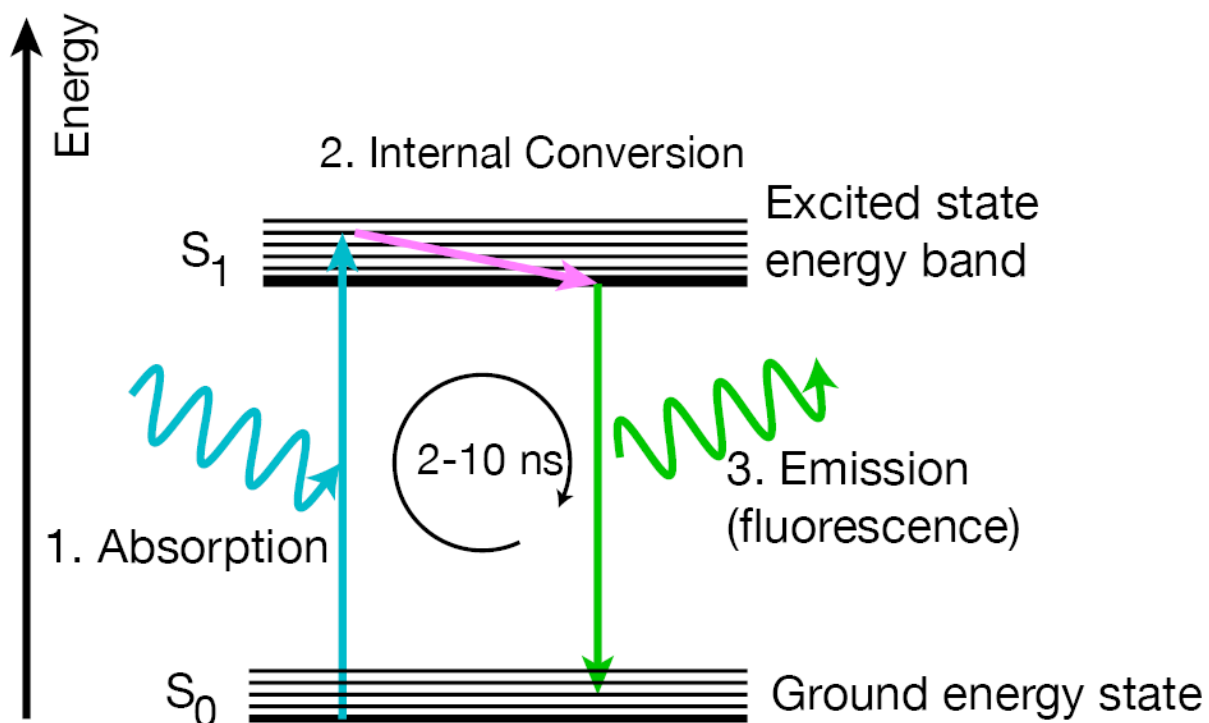
Shaner et al, Nature Biotechnology, 2004

DsRed	$\epsilon Q \sim 0.79 \times 75\,000 \sim 59\,250 M^{-1}.cm^{-1}$	(100%)
mRFP1	$\epsilon Q \sim 0.25 \times 50\,000 \sim 12\,500 M^{-1}.cm^{-1}$	(21%)
eGFP	$\epsilon Q \sim 0.6 \times 55\,000 \sim 33\,000 M^{-1}.cm^{-1}$	(56%)
Fluorescein	$\epsilon Q \sim 0.8 \times 70\,000 \sim 56\,000 M^{-1}.cm^{-1}$	(95%) (dye!)



# The dilute limit

Extinction coefficient and quantum yield corresponds to “well behaved” dye in the dilute limit: dilute photon and dilute dye



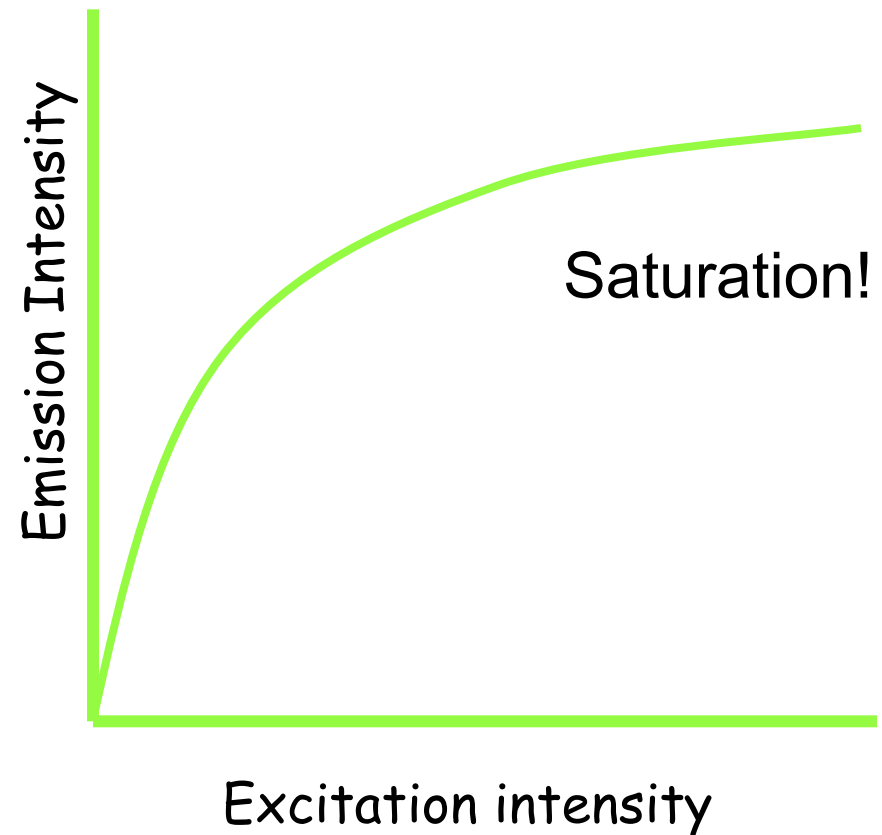
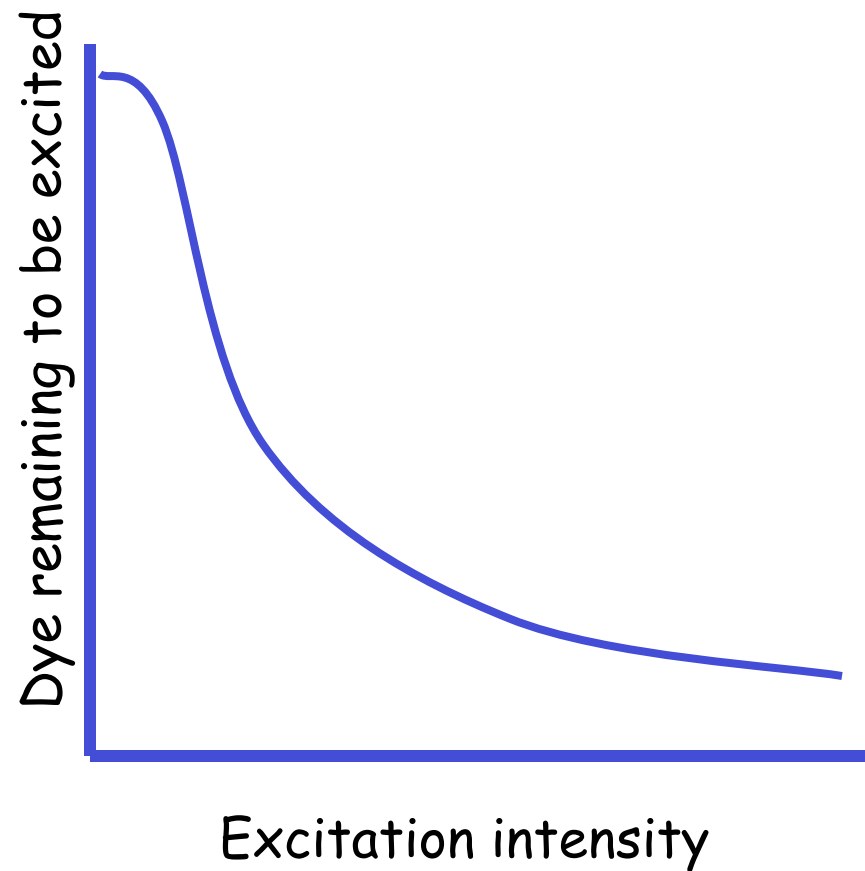
**Note:**

Fraction  $Q$ : Emission occurs

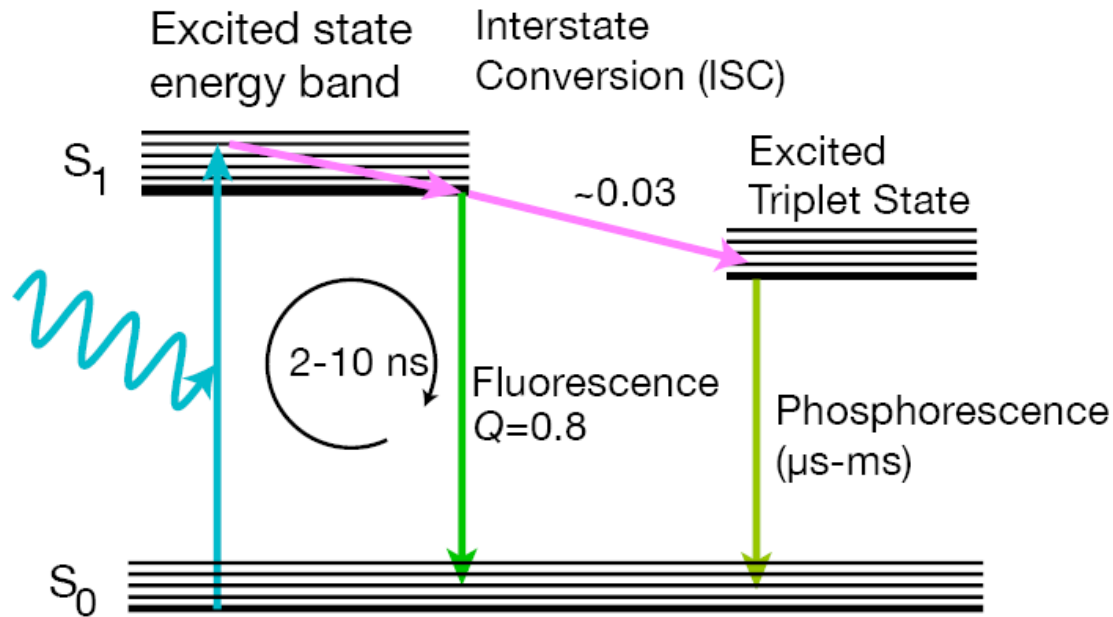
Fraction  $1 - Q$ : Other losses (heat and (non-radiative) energy transfer)

# The dilute limit: dilute photons

As photons hit specimen: dye molecules excited and less dye left unexcited



# Interstate crossing (ISC)



## Triplet state is long lived

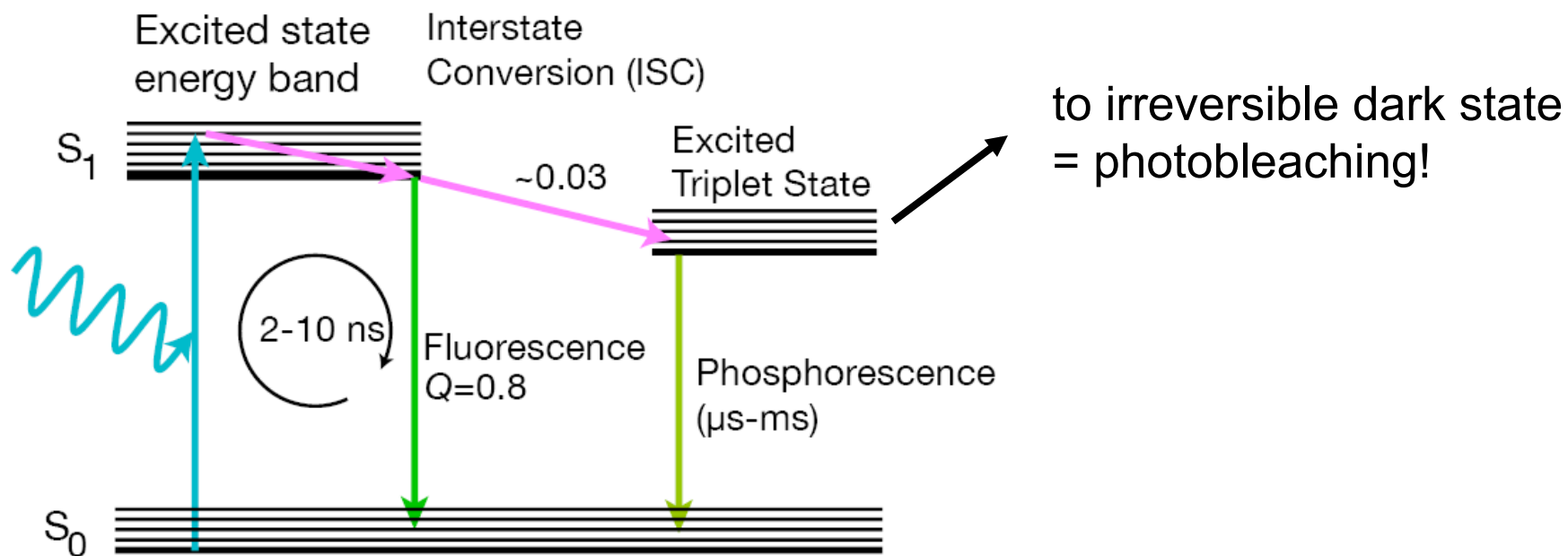
Even low probability can deplete active dye.

Probability of molecule in triplet state after  $N$  cycles:  $(1 - 0.03)^N = 0.97^N$   
( $N=10$ : 74%) Steady state reached in about 200ms

if 80-90% of molecules in triplet state: image is 5–10 fold dimmer

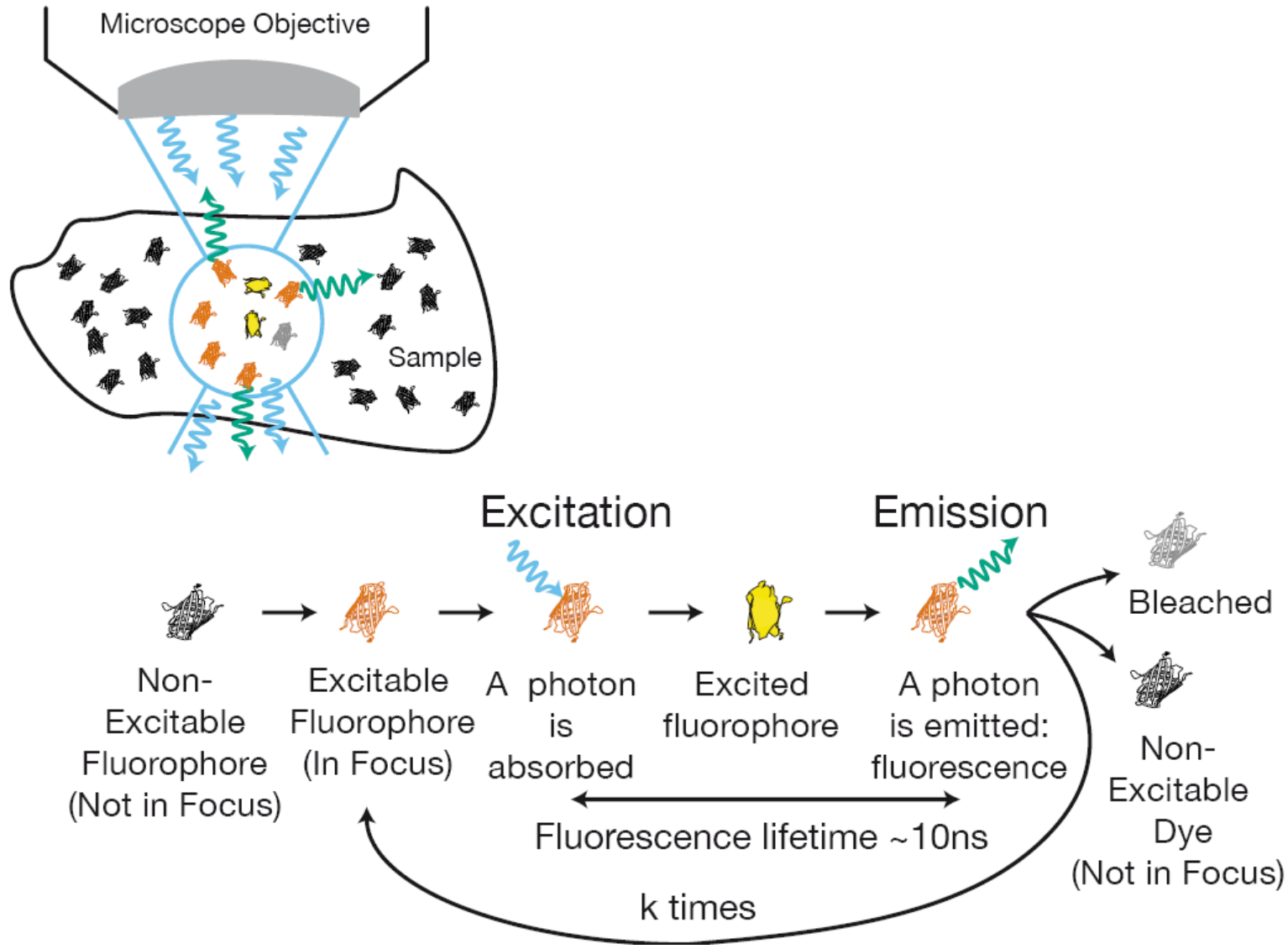
CLSM: can have major impact (about 5 fold less throughput)

# Interstate crossing (ISC) and photobleaching

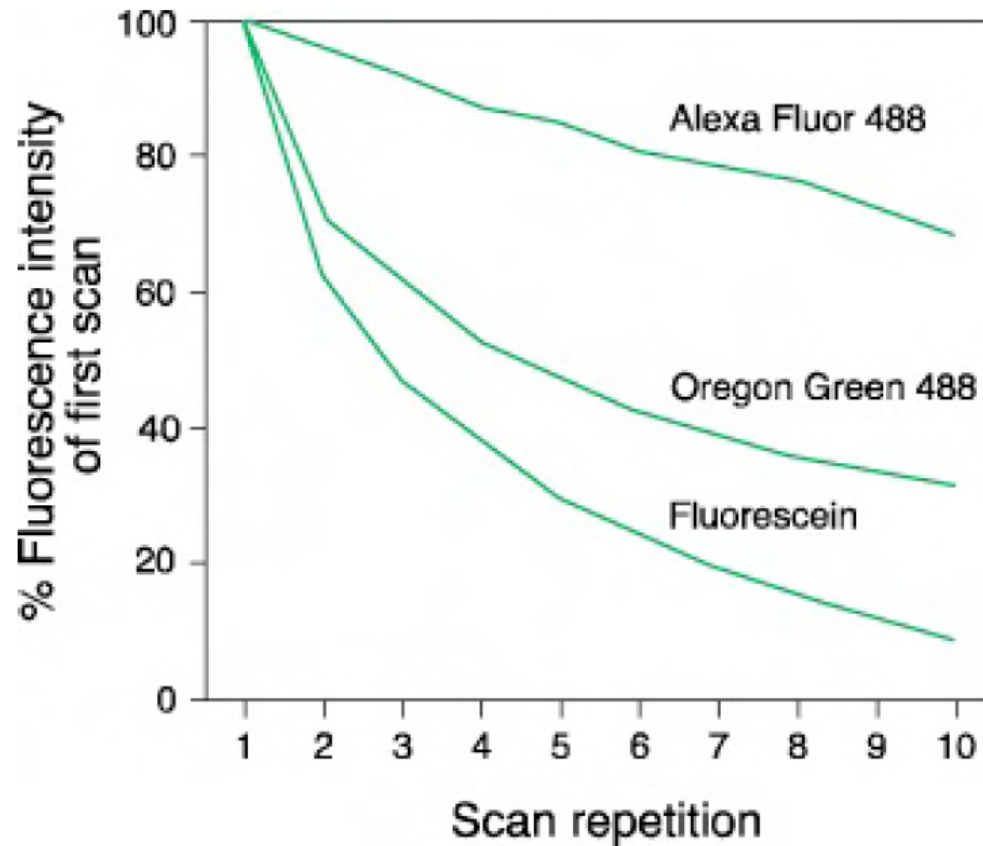


As ISC takes place: less dye molecules available and unexcitable dye accumulates

# Cycle of a fluorophore



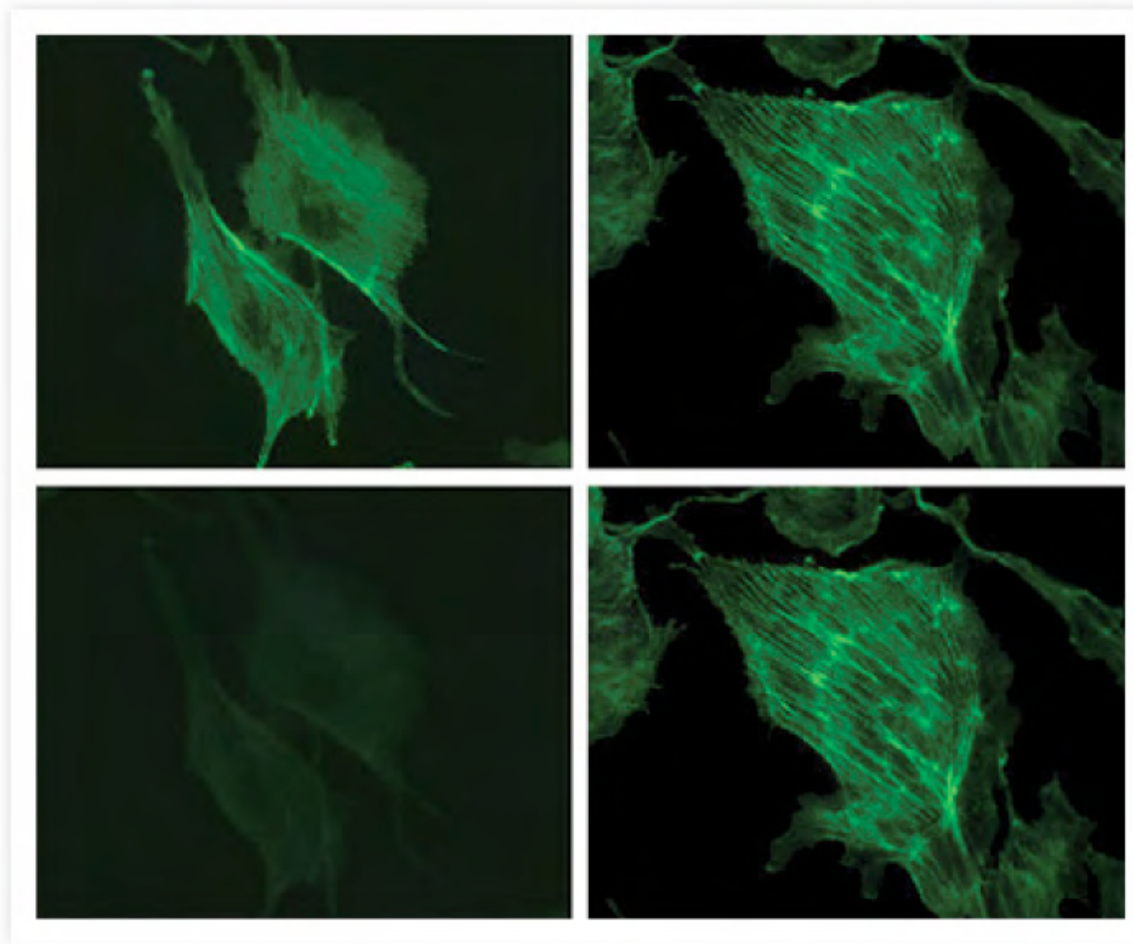
# Interstate crossing (ISC) and photobleaching



Photobleaching resistance of the green-fluorescent Alexa Fluor 488, Oregon Green 488 and fluorescein dyes, as determined by laser-scanning cytometry. EL4 cells were labeled with biotin-conjugated anti-CD44 antibody and detected by Alexa Fluor 488 (S11223), Oregon Green 488 (S6368) or fluorescein (S869) streptavidin (Section 7.6). The cells were then fixed in 1% paraformaldehyde, washed and wet-mounted. After mounting, cells were scanned 10 times on a laser-scanning cytometer; laser power levels were 25 mW for the 488 nm spectral line of the argon-ion laser. Scan durations were approximately five minutes apiece, and each repetition was started immediately after completion of the previous scan. Data are expressed as percentages derived from the mean fluorescence intensity (MFI) of each scan divided by the MFI of the first scan. Data contributed by Bill Telford, Experimental Transplantation and Immunology Branch, National Cancer Institute.

A good dye is more photostable (less photobleaching)

# Interstate crossing (ISC) and photobleaching



after 30 seconds

Bovine pulmonary artery endothelial cells (BPAEC) were labeled with fluorescein phalloidin (left panels, F432), or Alexa Fluor 488 phalloidin (right panels, A12379), which labels filamentous actin, and mounted in PBS. The cells were placed under constant illumination on the microscope with an FITC filter set using a 60 objective. Images were acquired at one-second intervals for 30 seconds. Under these illumination conditions, fluorescein photobleached to about 20% of its initial value in 30 seconds; the fluorescence of Alexa Fluor 488 phalloidin stayed at the initial value under the same illumination conditions.

Source: <http://probes.invitrogen.com/servlets/photo?fileid=g001270&company=probes>

# Photobleaching characterization

## Example: properties of fluorescent protein variants

**Table 1 Properties of novel fluorescent protein variants**

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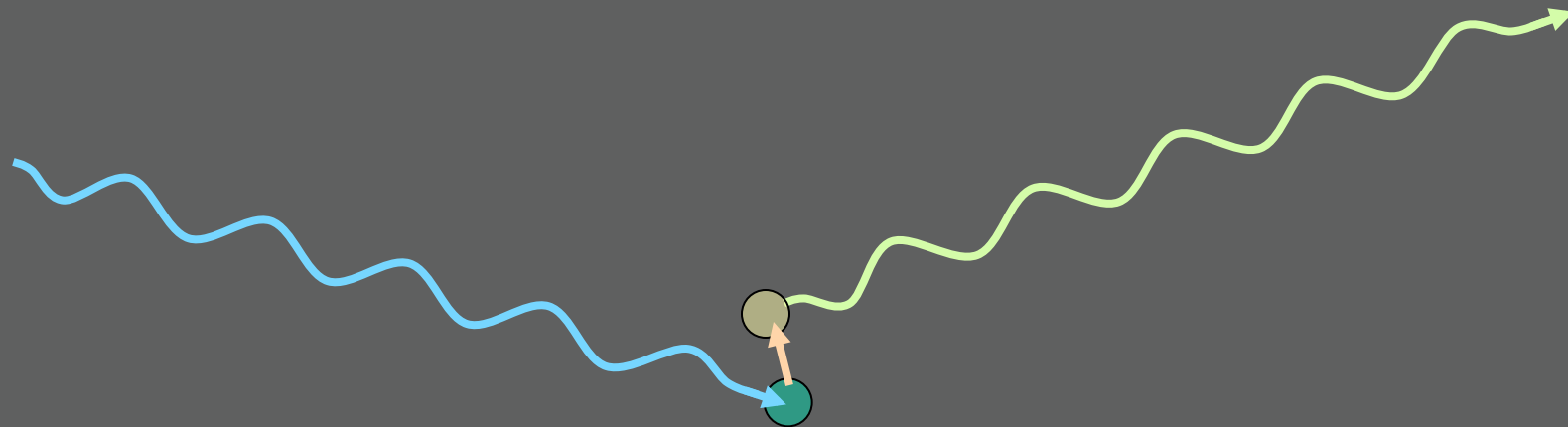
<sup>a</sup>Extinction coefficients were measured by the alkali denaturation method<sup>8,30</sup> and are believed to be more accurate than the previously reported values for DsRed, T1, dimer2 and mRFP1<sup>7</sup>.

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Shaner et al, Nature Biotechnology, 2004



# Resonance Energy Transfer (non-radiative)



Transfer of energy from one dye to another

Depends on:

Spectral overlap

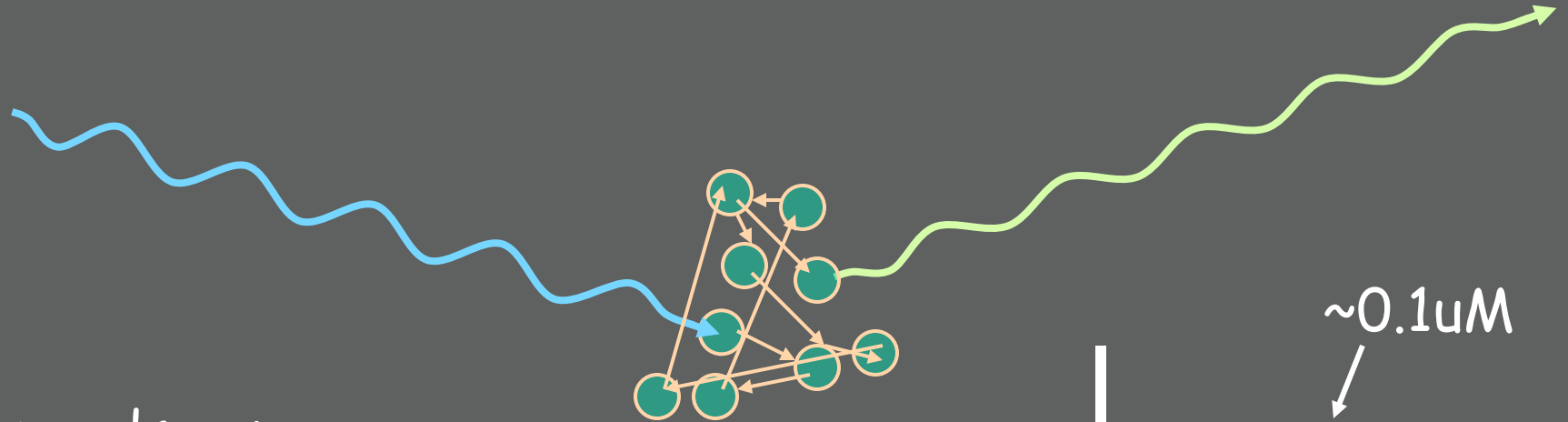
Distance

Alignment

FRET is not always between dissimilar dyes

“Self-quenching” of dye

(“hot-potato” the energy until lost)



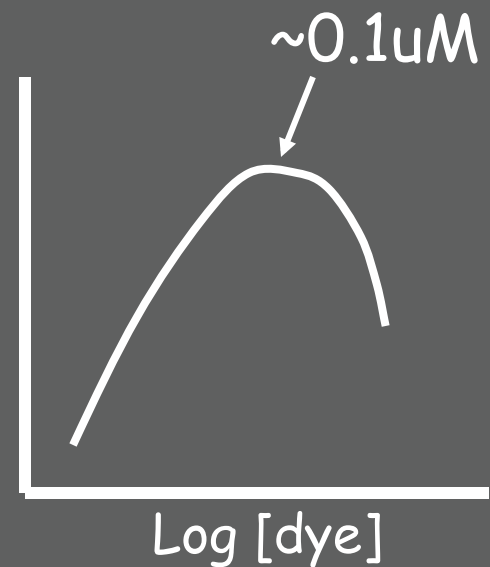
Depends on:

Dye Concentration

Geometry

Environment

Log I

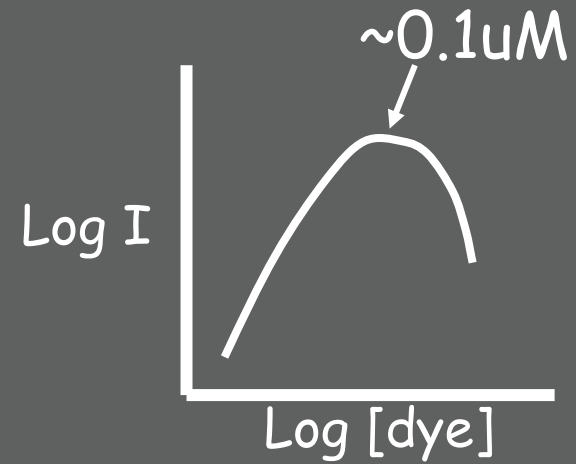


# “Self-quenching” of dye

Depends on:

Dye Concentration

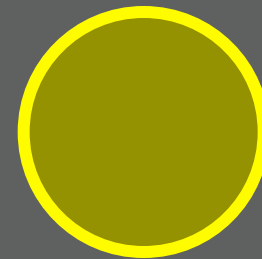
Geometry



Hard for emission from this one



A uniformly dyed structure

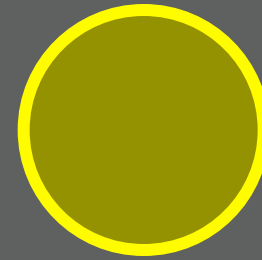


Instead, looks “hollow”

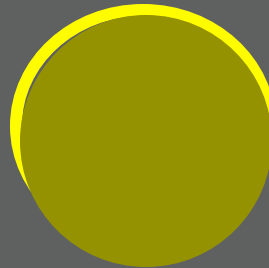
If structure large enough, collection efficiency not equivalent for top, side, bottom



A uniformly dyed structure

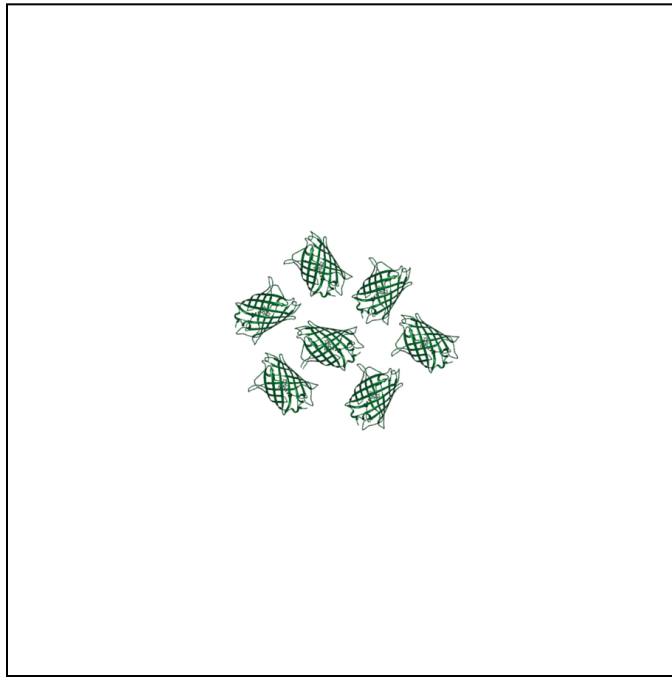


Instead, looks "hollow"

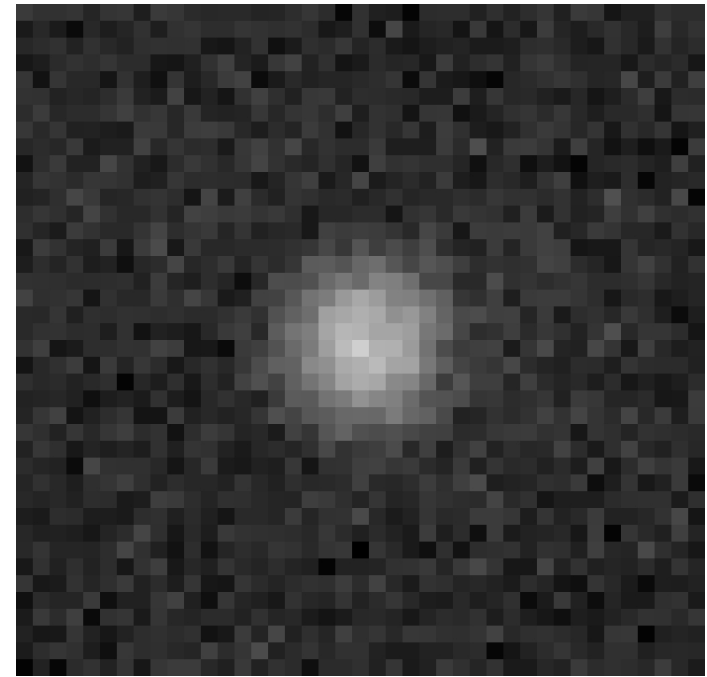


Can even become a crescent

# Fluorescence quantification based on signal intensity



input: [fluorophore]



Output: pixel grey levels

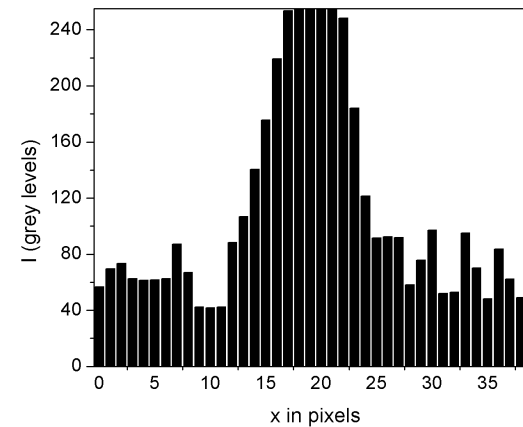
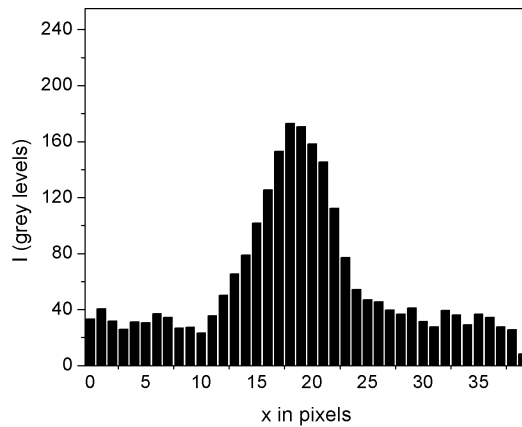
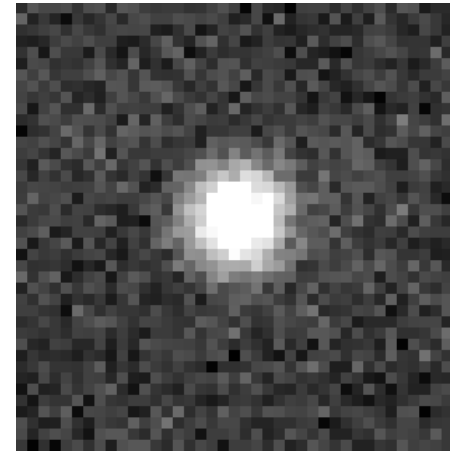
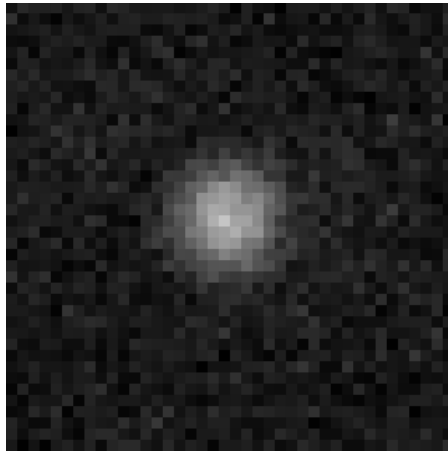
Example:

in = level of expression of a fluorescent protein

out = fluorescent signal and grey level of pixel on an image.

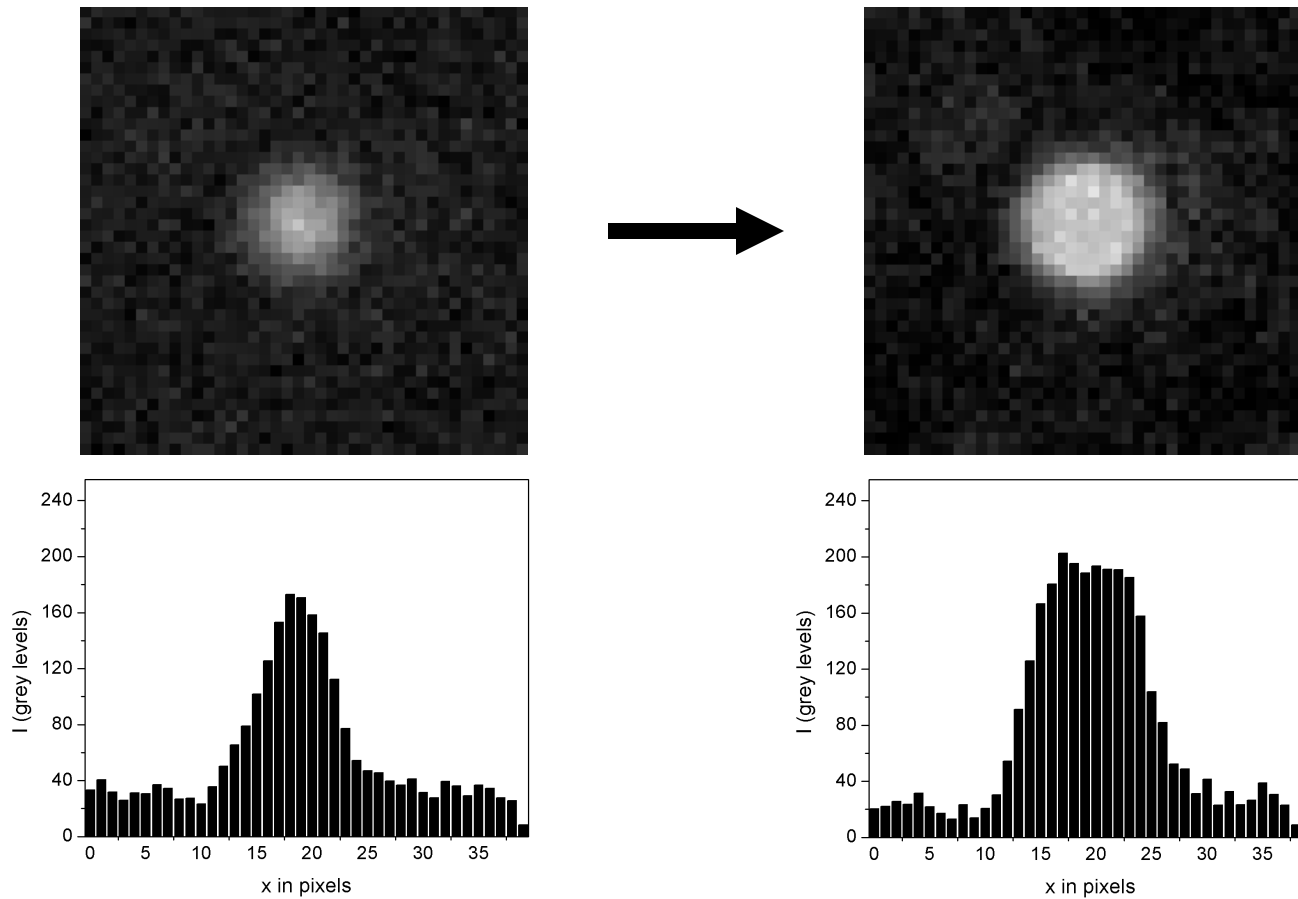
# Example of nonlinearity: pixel saturation

(detector or digital contrast)



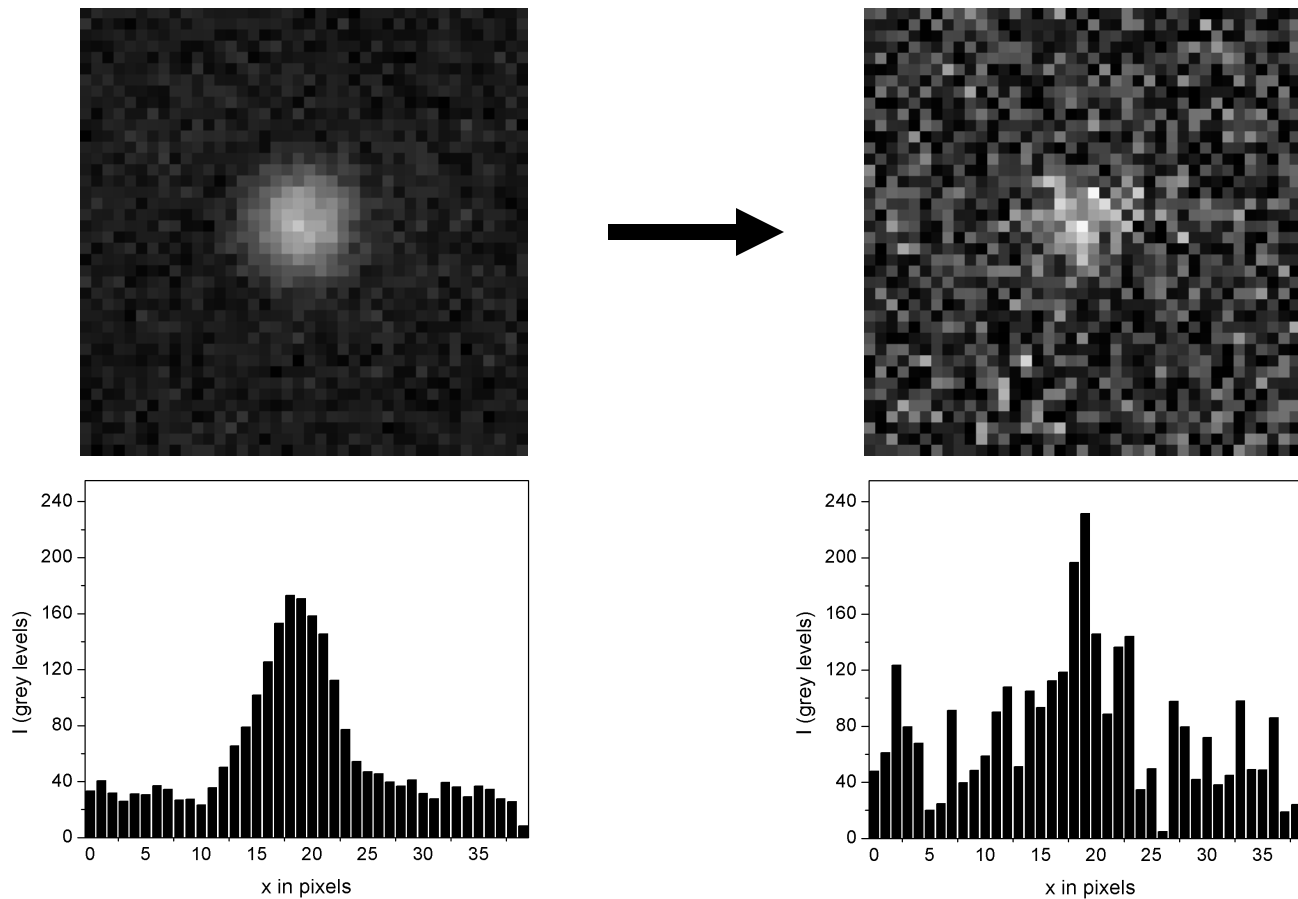
Solution(s): use less power!!!, decrease the acquisition time, decrease [fluorophore],...

# Example of nonlinearity: fluorophore saturation



Solution(s): use less power!!!, decrease the acquisition time,...

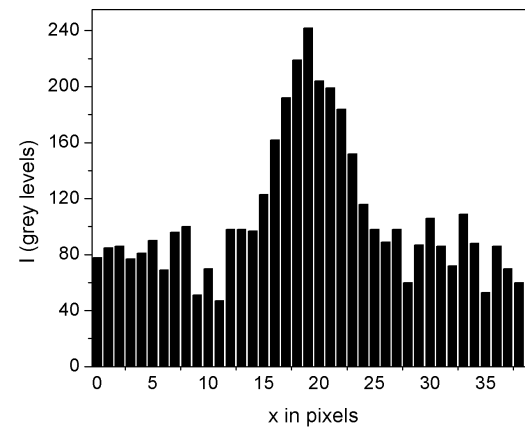
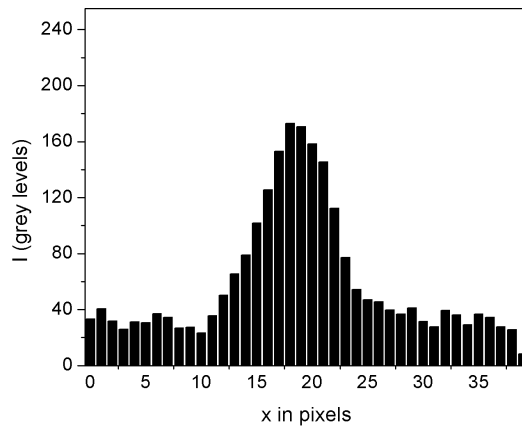
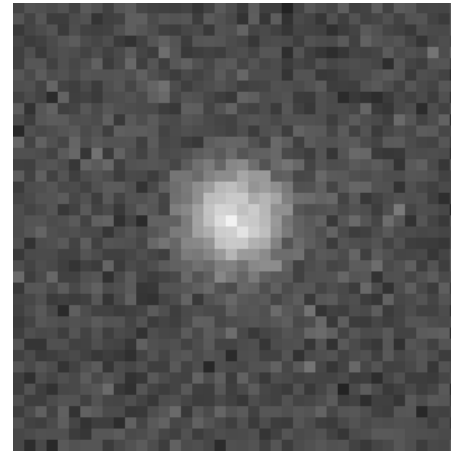
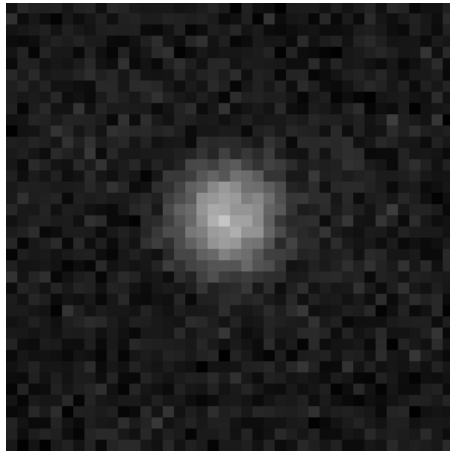
# Example of nonlinearity: noise



Solution(s): optimize the excitation wavelength, increase the acquisition time, use more power, use a stronger fluorophore, increase [fluorophore],...



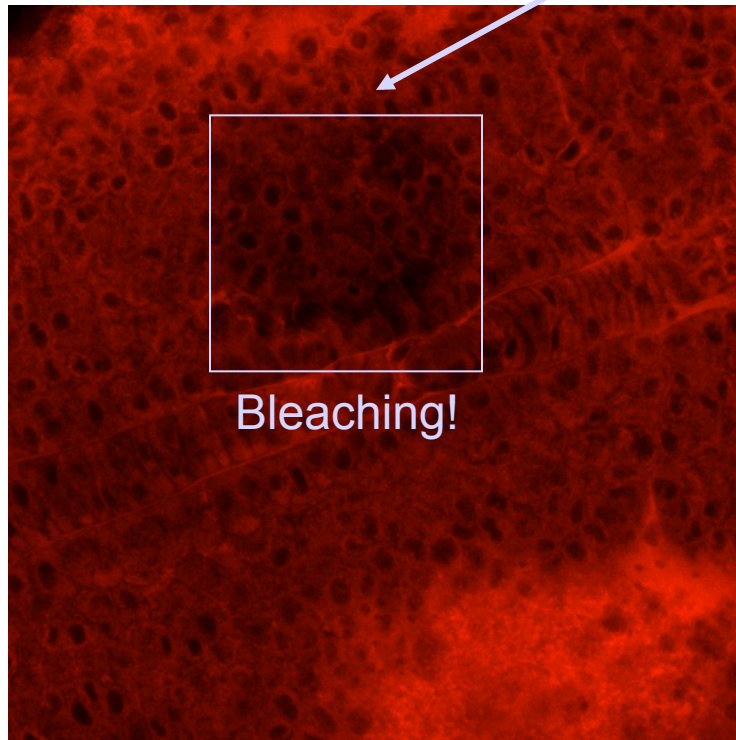
# Example of nonlinearity: photo-induced fluorescence



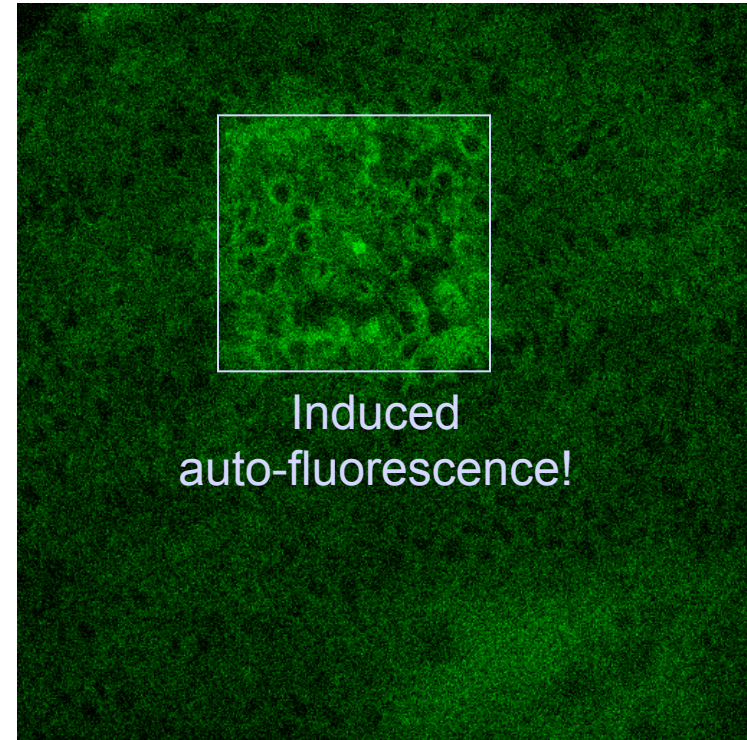
Solution: use less power!

# Example of nonlinearity: photo-induced fluorescence

zoom out after imaging in this area



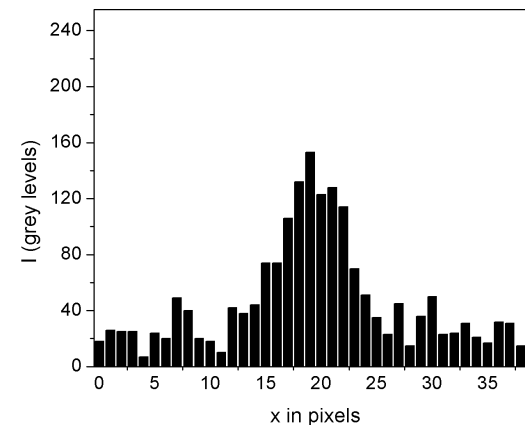
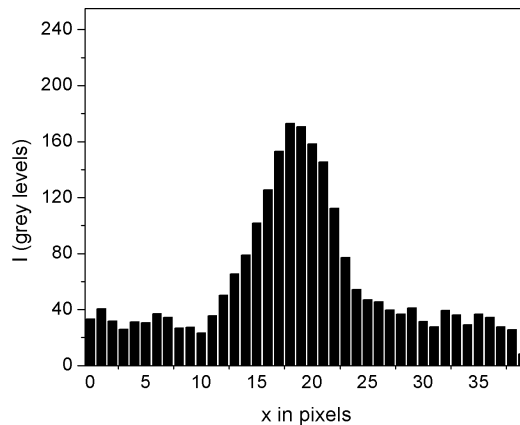
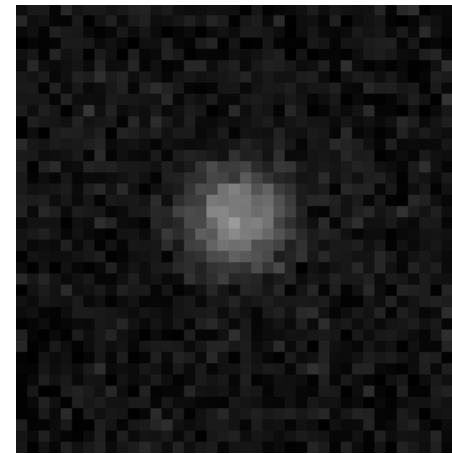
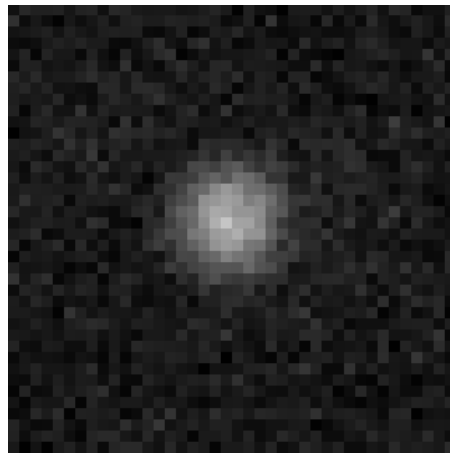
Red channel



Green channel

# Compare what is comparable: imaging depth

Same object imaged at different tissue depth...



The fluorescence level depends on  
the depth of imaging and the optical properties of the the tissue  
(variation from one sample to another)...

All dyes look redder as you look deeper in tissue

# How to protect yourself from non-linearities?

You can't - but you can look for diagnostic defects

- Edges to structures
- Asymmetries in intensity

Test: reduce laser; does image reduce proportionately?

Avoid over-labeling

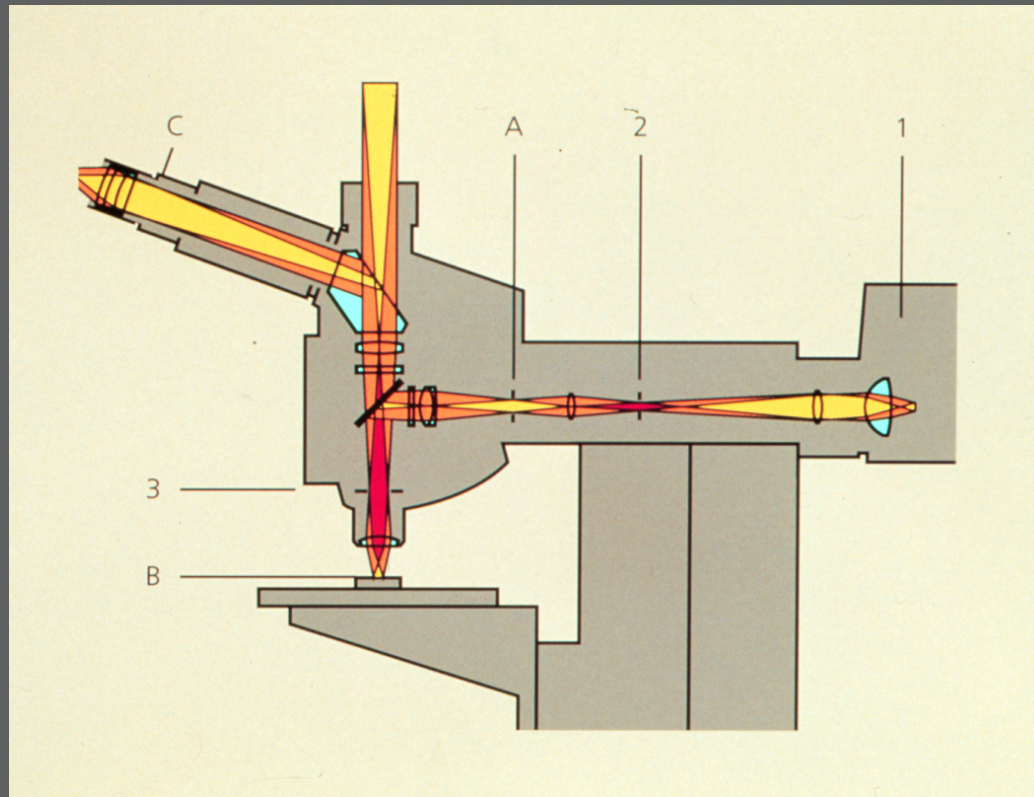
Avoid over-stimulating

“When in doubt, reduce intensity of stimulation”

# Microscope has non-linearities

Camera

Relay optics

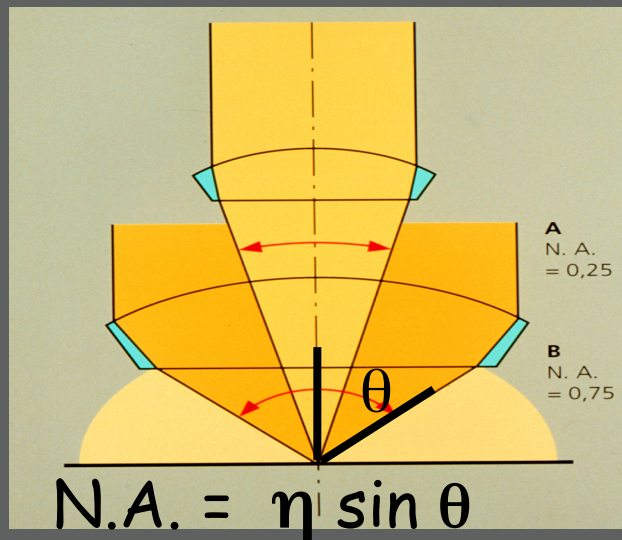


Eyepieces

Objective

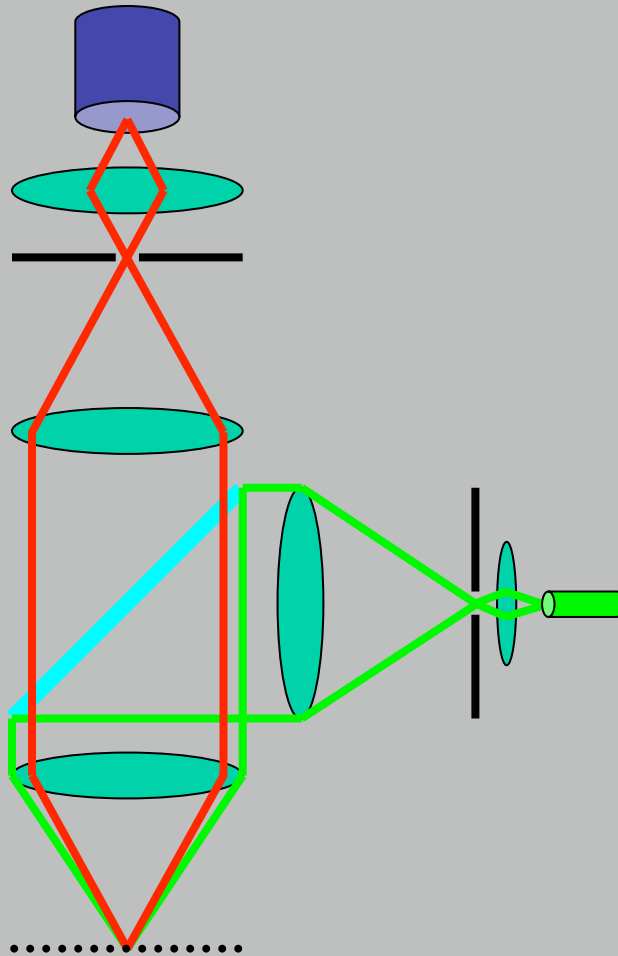
light source  
(image of arc)

Objective lens better at collecting light near center



# No free lunch from Confocal

Good: Single detector



Good: Single light source

Bad: very sensitive to optical aberrations

Bad: Easy to saturate dye (less excitation, ISC)

# Spherical Aberration



The image cannot be displayed. Your computer may not have enough memory to open the image, or the image may have been corrupted. Restart your computer, and then open the file again. If the red x still appears, you may have to delete the image and then insert it again.

# Lateral Chromatic Aberration



The image cannot be displayed. Your computer may not have enough memory to open the image, or the image may have been corrupted. Restart your computer, and then open the file again. If the red x still appears, you may have to delete the image and then insert it again.

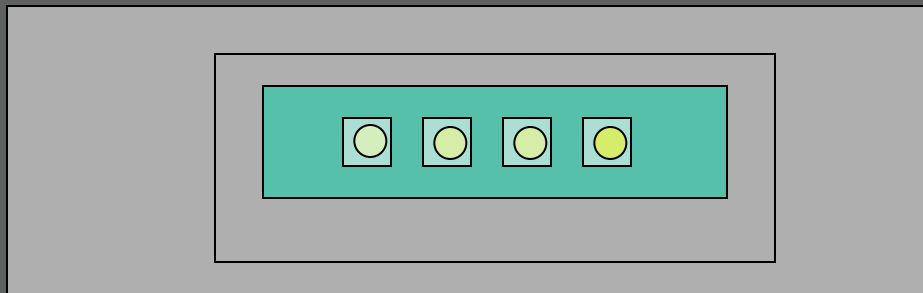


## Solution: Flat Fielding (pixel by pixel correction)

### Requirements:

Specimen of uniform intensity

Set of specimens of different known brightness



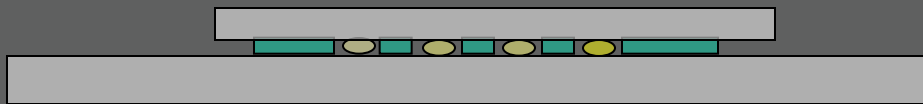
Slide with double-stick tape

Cut holes in tape

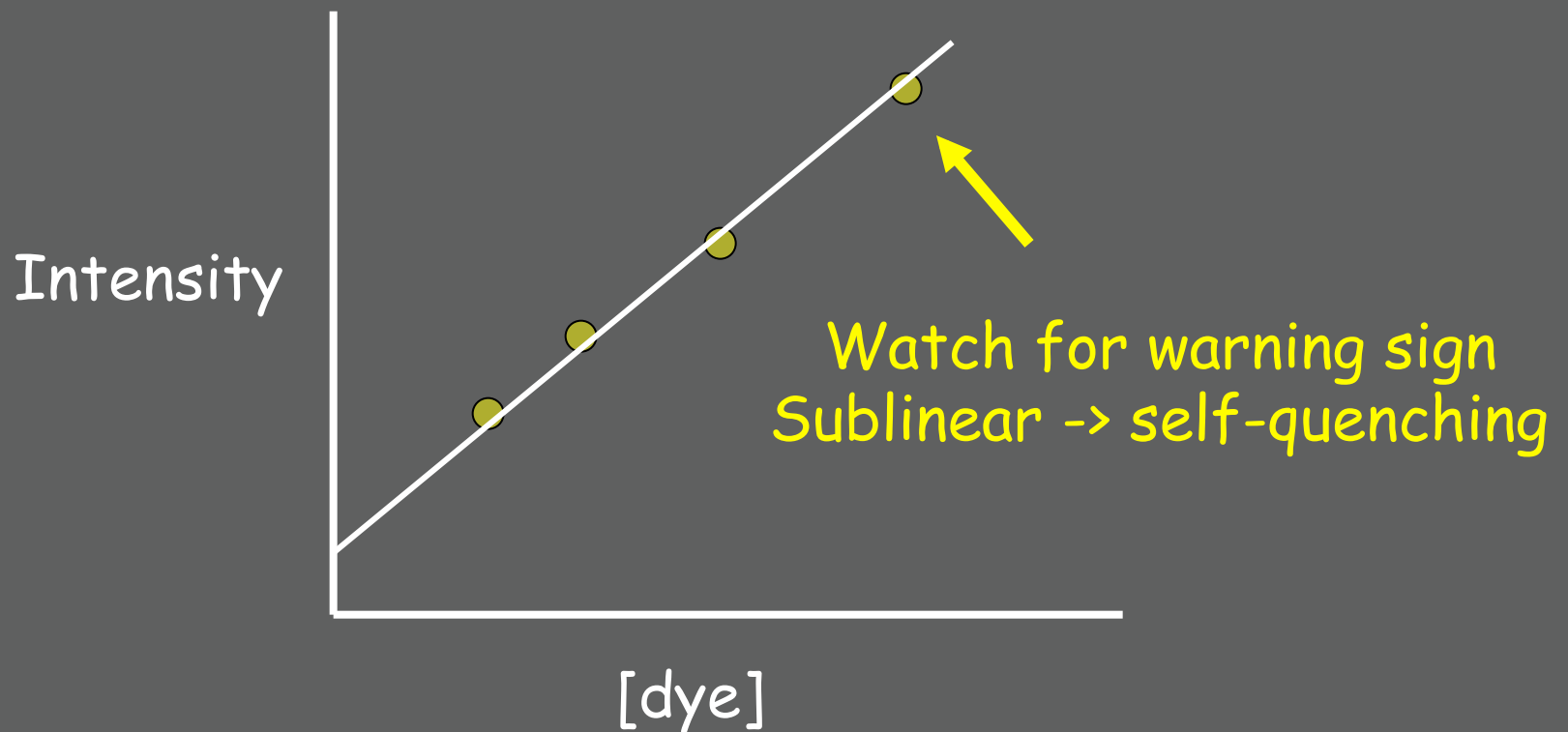
Drop dye in holes

Different [dye] in each hole

Coverslip over the top

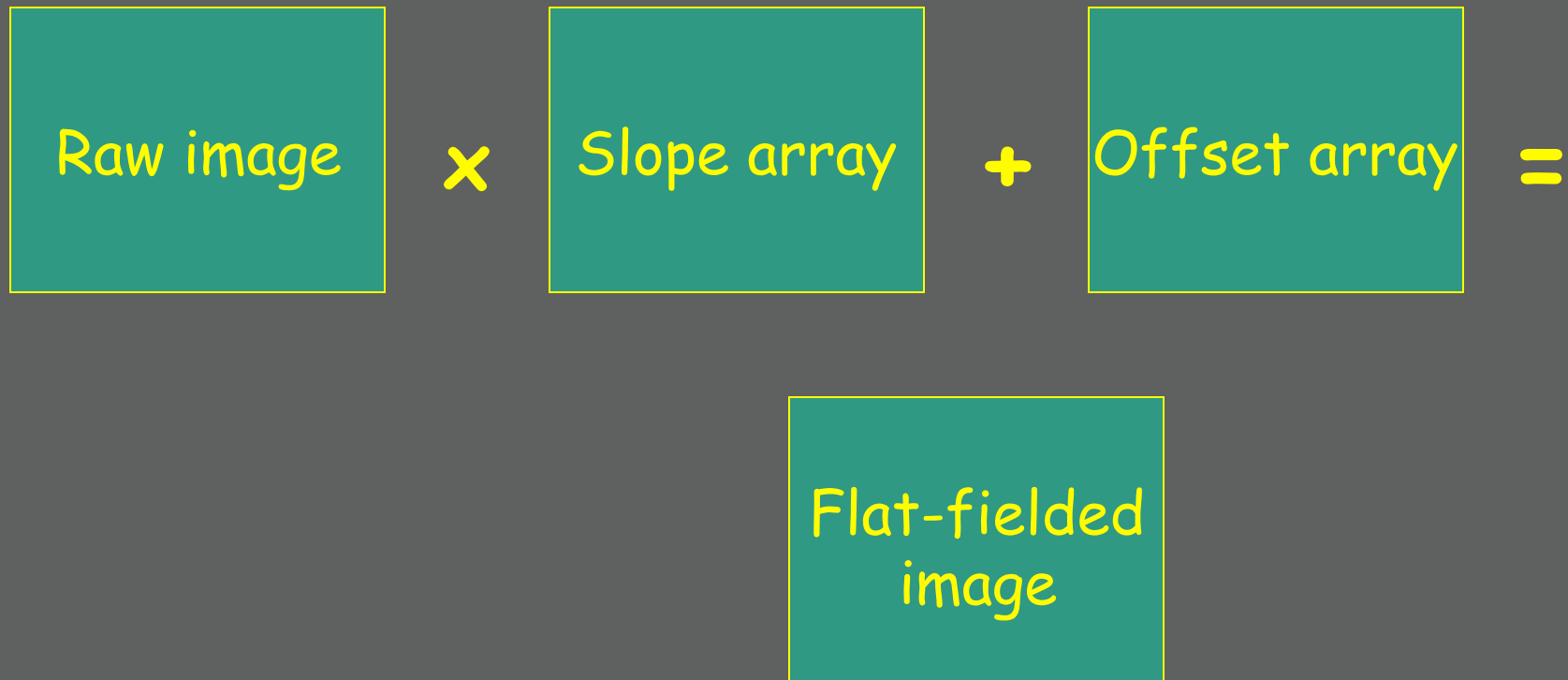


On pixel by pixel basis  
Plot I vs [dye]  
Calculate slope & intercept



References:

Kindler & Kennedy (1996) *J Neurosci Methods* 68:61-70  
Stollberg & Fraser (1988) *J Cell Biol* 107: 1397-1408.



References:

- Kindler & Kennedy (1996) *J Neurosci Methods* 68:61-70  
Stollberg & Fraser (1988) *J Cell Biol* 107: 1397-1408.

So how many fluors does a given intensity equal?

**Single-molecule measurements calibrate green  
fluorescent protein surface densities on transparent  
beads for use with “knock-in” animals**

Chi-Sung Chiu<sup>1</sup>, Emil Kartalov<sup>2</sup>, Marc Unger<sup>2</sup>, Stephen Quake<sup>2</sup>, and Henry A. Lester<sup>1</sup>

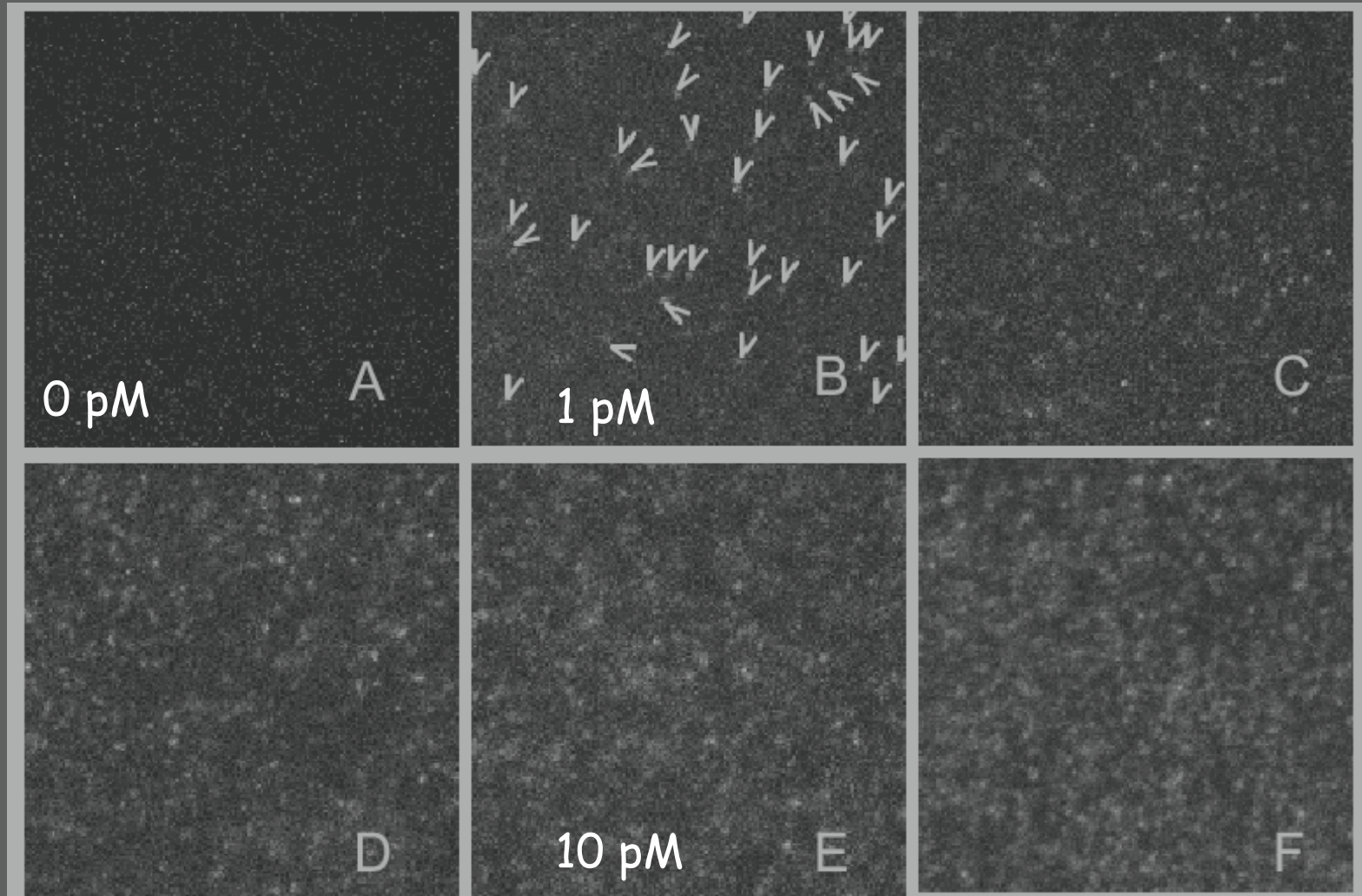
Divisions of <sup>1</sup>Biology and <sup>2</sup>Applied Physics, California Institute of Technology, Pasadena

CA 91125

Running title: Beads with calibrated GFP surface densities

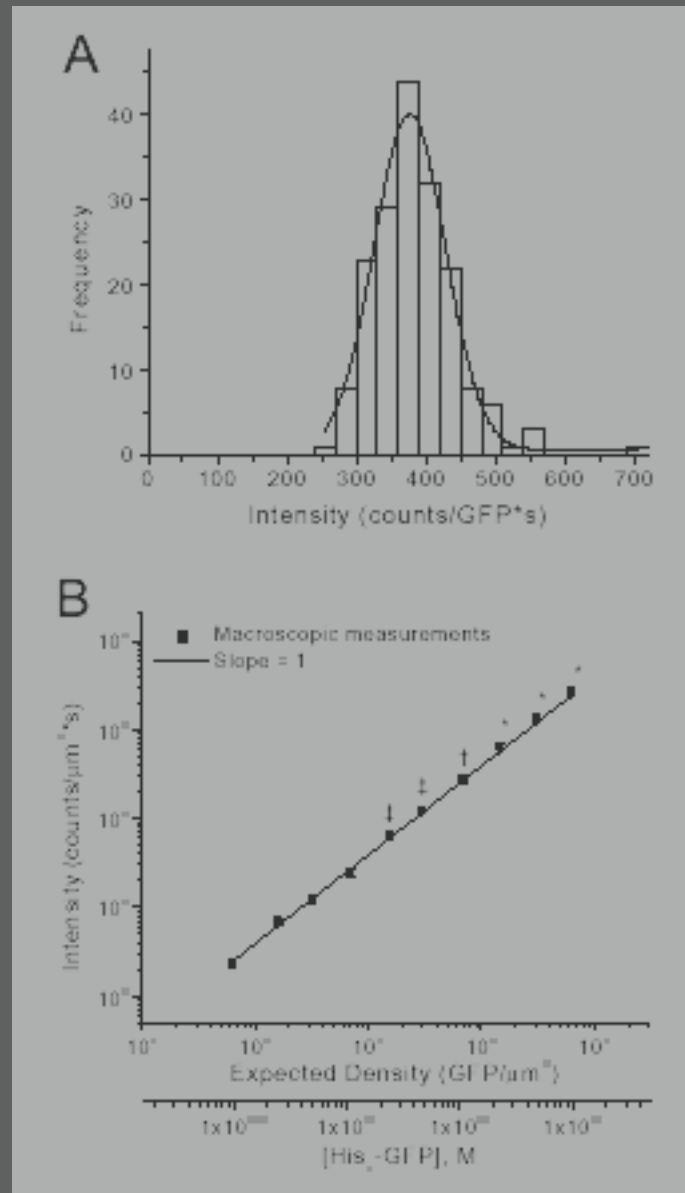
J Neurosci Methods 105:55-63 (2001)

## Beads with Ni-NTA; GFP::His<sub>6</sub>



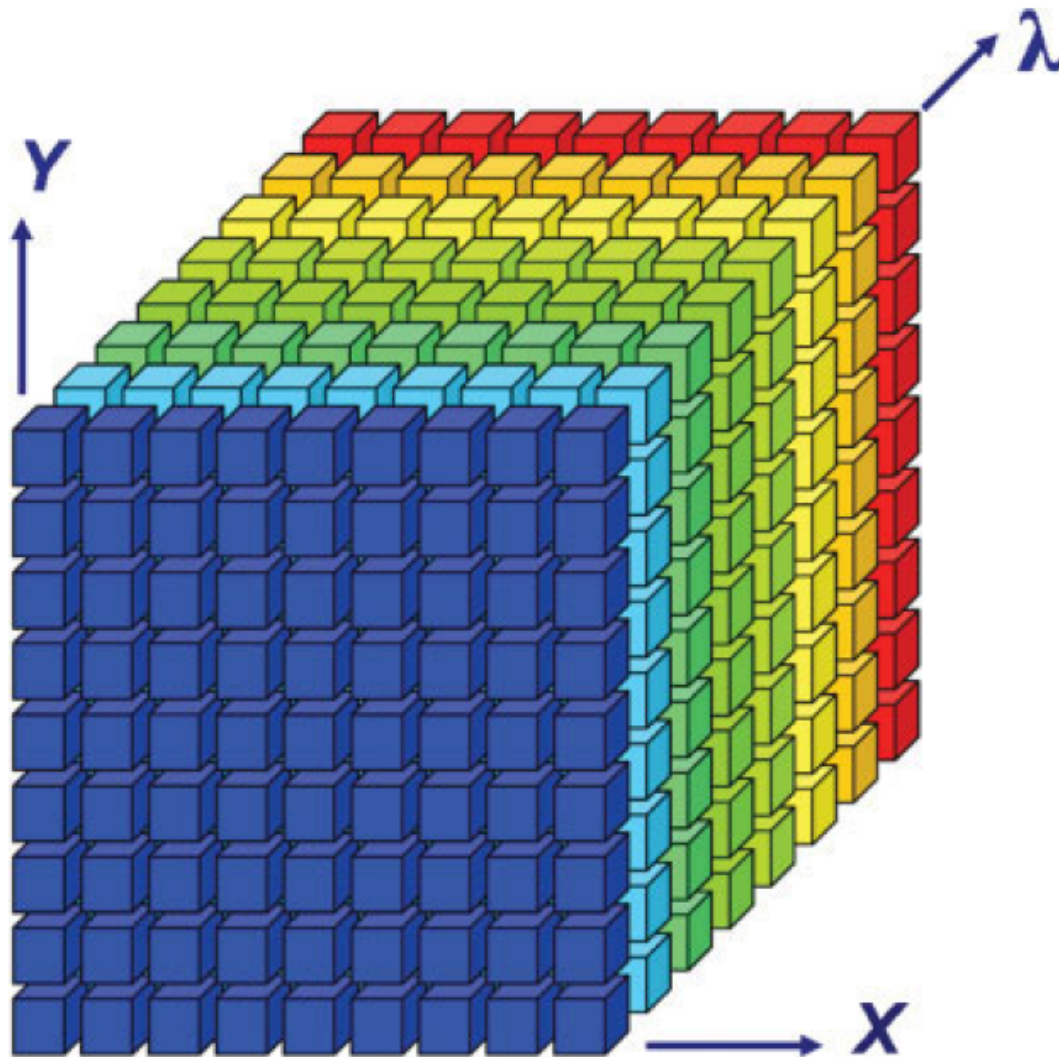
*J Neurosci Methods* 105:55-63 (2001)

Alternative: use viruses with defined numbers of GFP's



J Neurosci Methods 105:55-63 (2001)

# Spectral image dataset



$\lambda$ -stack

$\lambda$  can be:

(i)  $\lambda_{\text{excitation}}$   
*images acquired in a single channel at different  $\lambda_{\text{excitation}}$*

(ii)  $\lambda_{\text{emission}}$   
*images acquired at a single  $\lambda_{\text{excitation}}$  in several channels at different ( $\lambda_{\text{emission}}$ )*

FIG. 2. Description of a spectral image data set. Each point in the cube represents a single number and the spectral image is described as  $I(x,y,\lambda)$ . It can be viewed either as an image  $I(x,y)$  at each wavelength  $\lambda$ , or as a spectrum  $I(\lambda)$  at every pixel  $(x,y)$ .

# Spectral image dataset

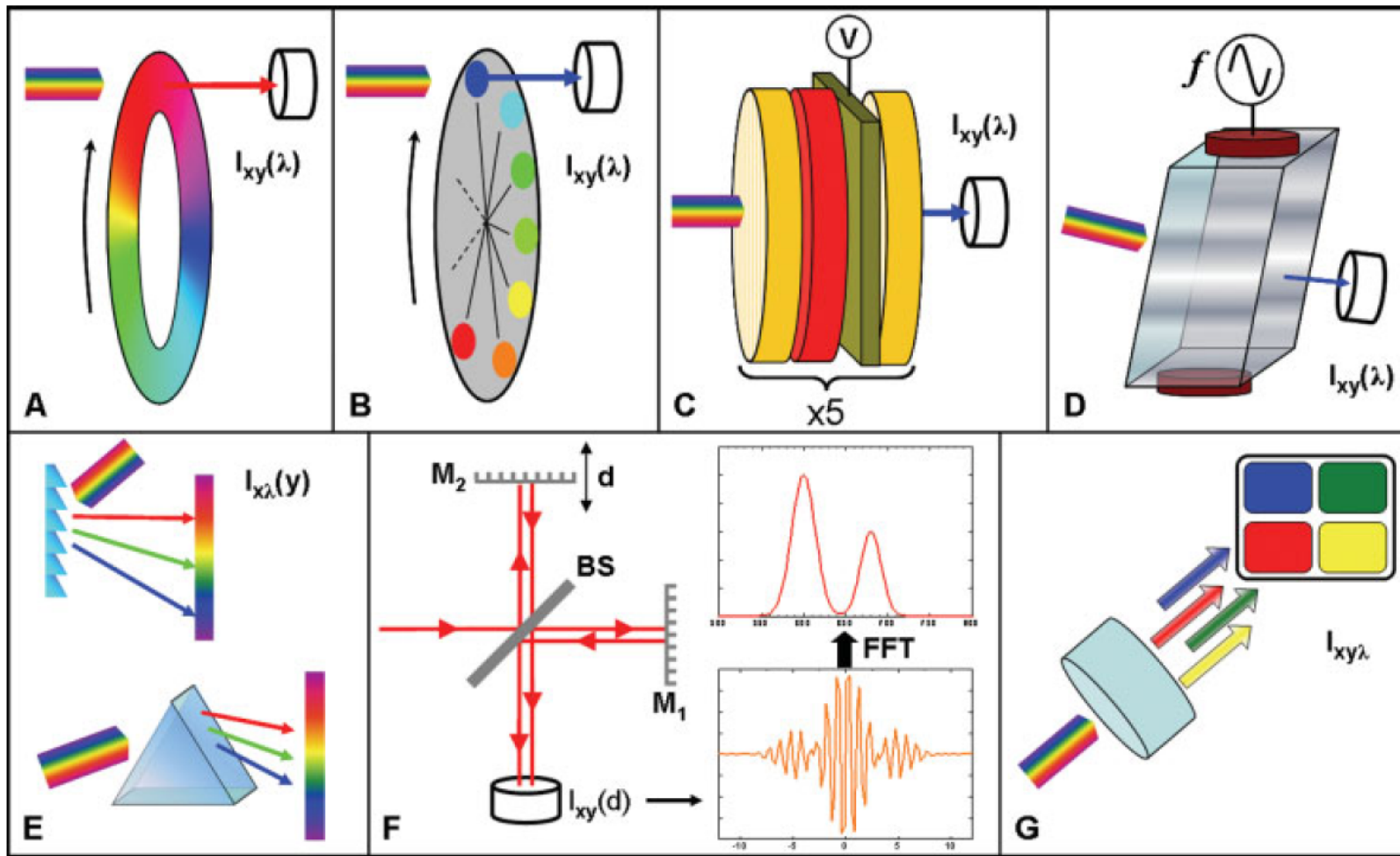
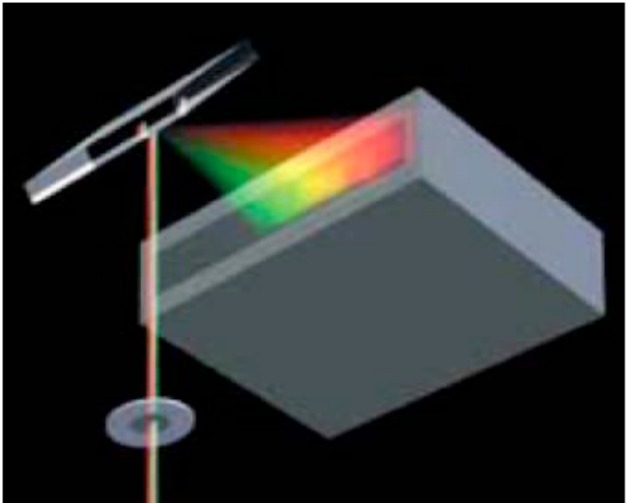
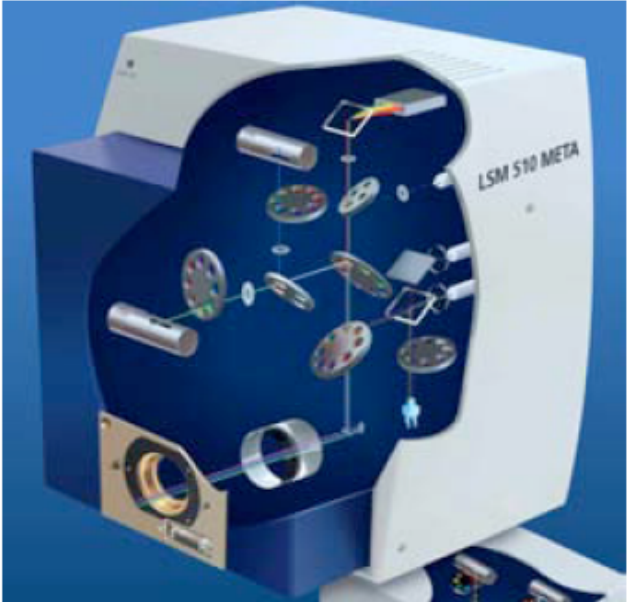
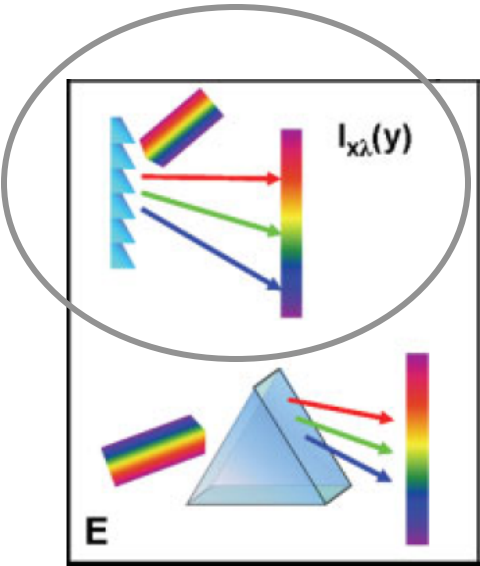


FIG. 3. Various methods of spectral imaging systems. They can be divided into four main methods: wavelength-scan (A-D), spatial scan (E), time scan (F) and “compromise” methods (G). In wavelength-scan methods, the whole image is measured one wavelength at a time. This can be realized using either a circular variable filter (A), a set of filters (B), a liquid crystal variable filter (C) or an acousto-optic variable filter (D). Spatial-scan methods use a dispersion element, either a grating or prism (E) and the image has to be scanned along at least one axis. There are also confocal microscopes that use a dispersive element and scan the image point by point. In time-scanning method (F), the whole image is measured after passing through an interferometer (or other optical elements). In order to calculate the spectrum at each pixel a mathematical transformation has to be carried out, for example, a Fourier transform. In “compromise” methods (G) only a few spectral ranges are measured and the FOV is limited, but the measurement is fast.



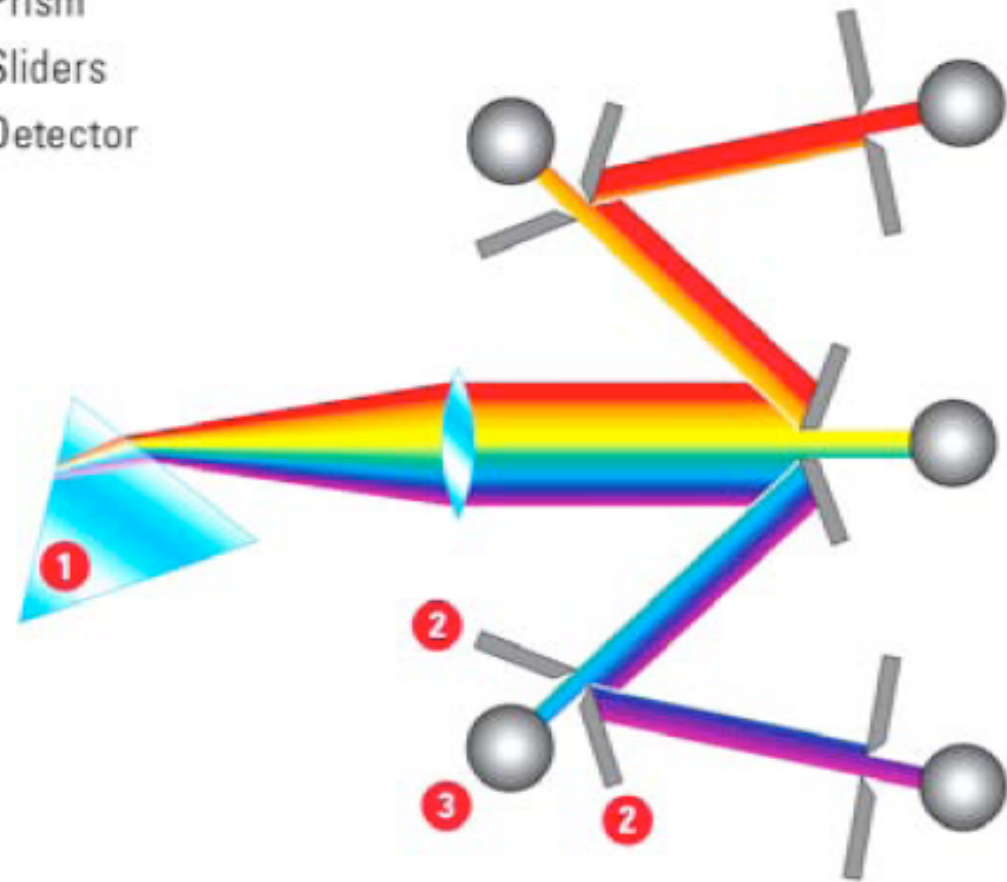
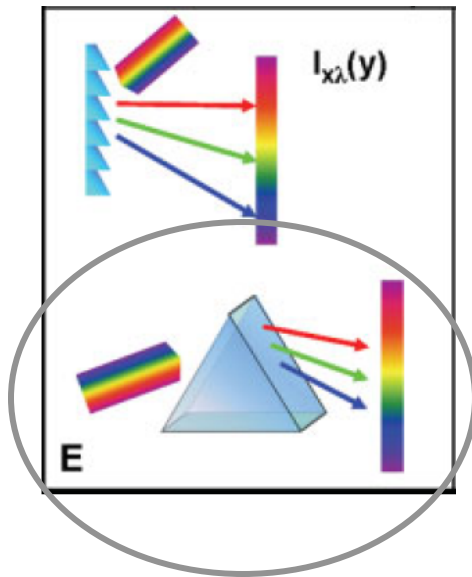
# Spectral imaging with a grating



Source: Carl Zeiss, GmbH

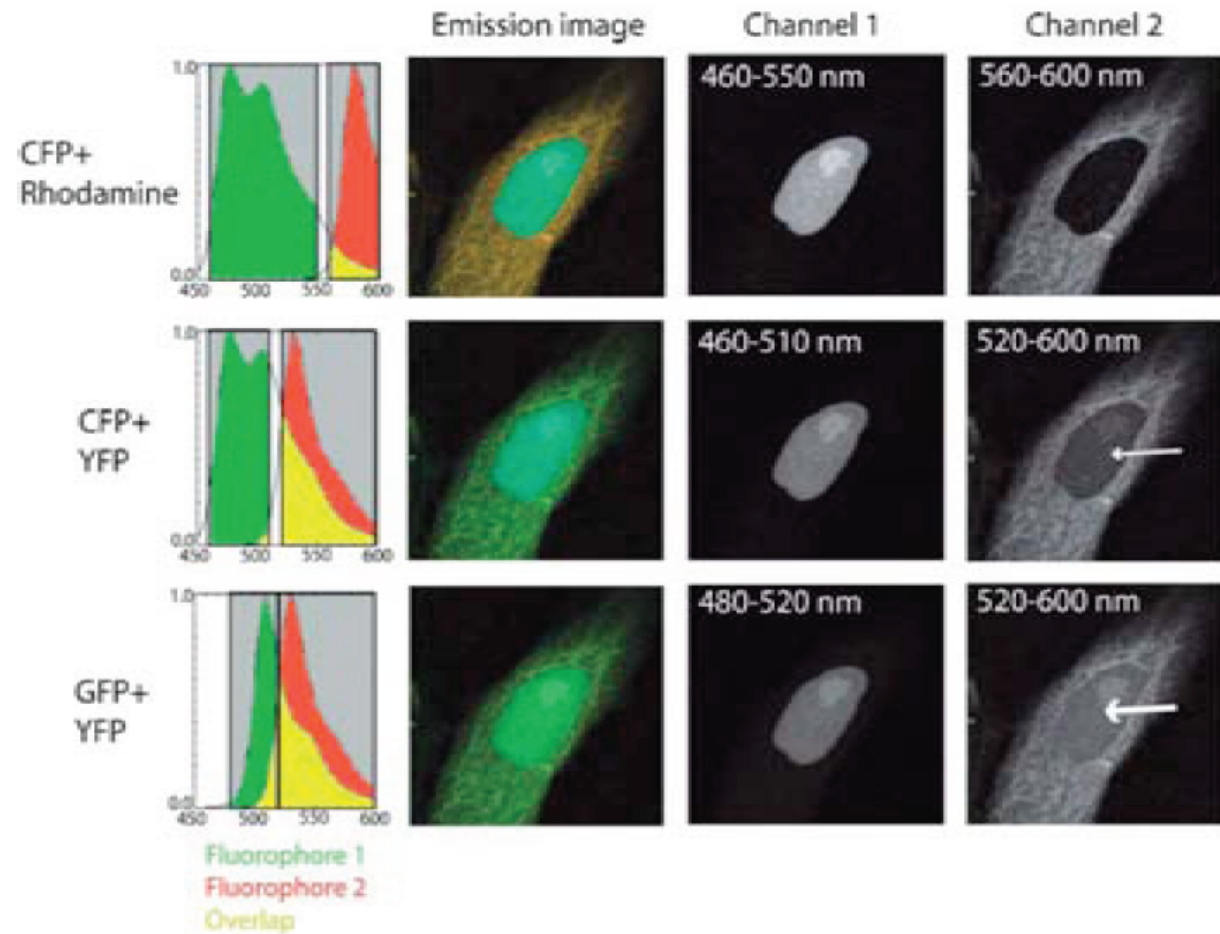
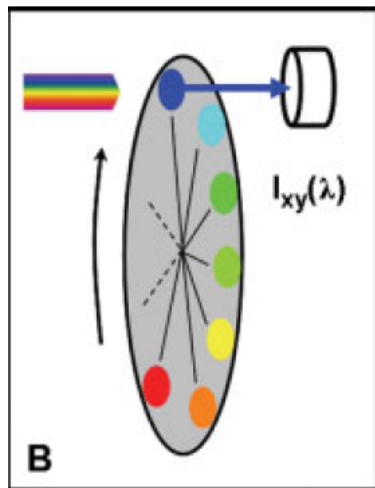
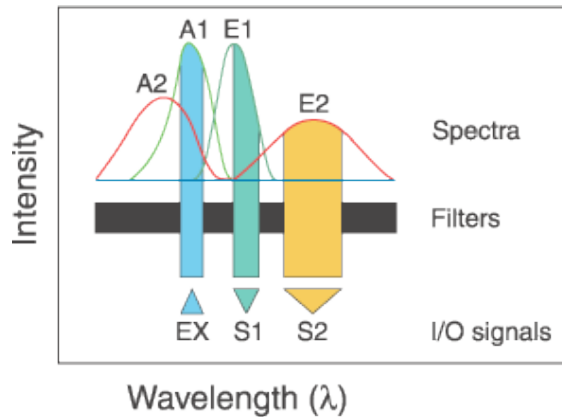
# Spectral imaging with a prism and mirrors

- 1 Prism
- 2 Sliders
- 3 Detector



Source: Leica

# Choose spectrally well-separated dyes

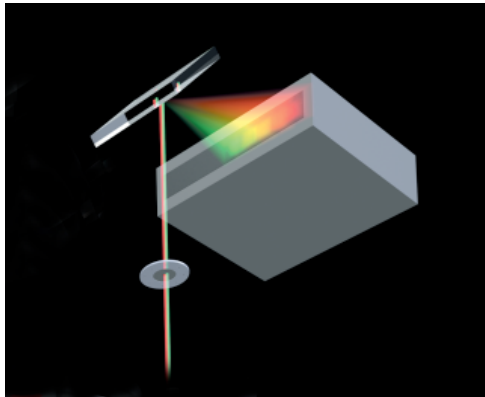


Source: T. Zimmermann, "Spectral Imaging and Linear Unmixing," Adv Biochem Engin/Biotechnol (2005) 95: 245–265

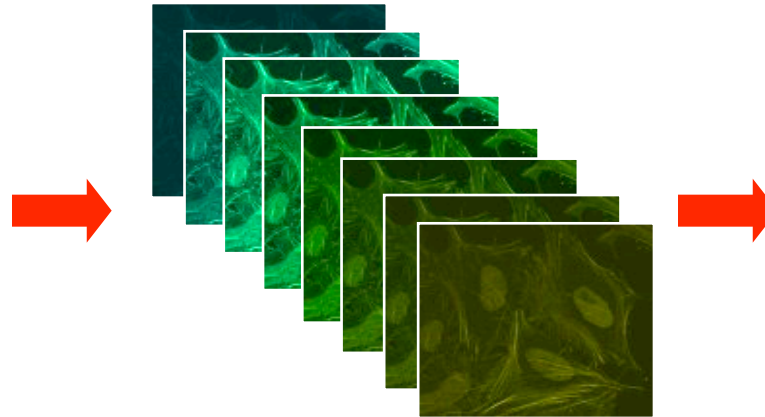
if not possible: use spectral unmixing!

# Spectral unmixing: general concept

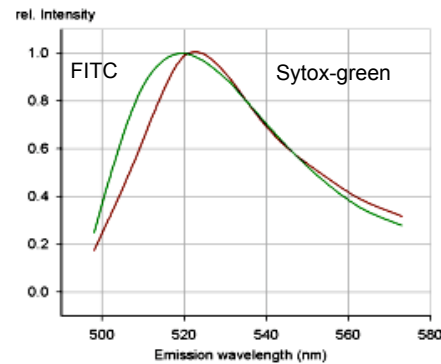
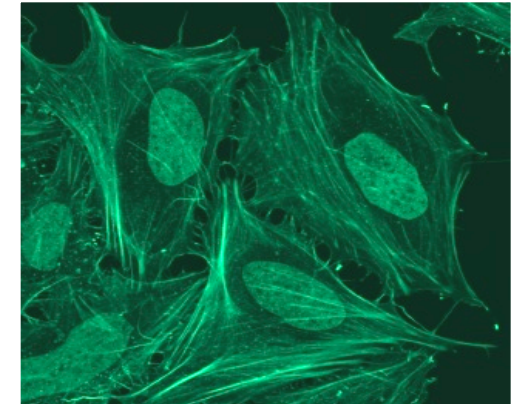
**Multi-channel  
Detector**



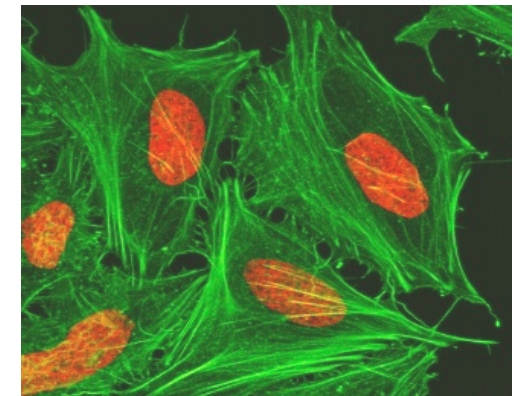
**Collect Lambda  
Stack**



**Raw Image**



**Derive Emission  
Fingerprints**



**Unmixed Image**

# Linear spectral unmixing: principle

Signal of a sample containing  $N$  fluorophores:

$$S(\lambda) = \sum_{i=1}^N A_i R_i(\lambda)$$

where  $A_i$ : relative contribution by specific fluorophore  $i$  with reference spectrum  $R_i(\lambda)$ .

If spectrum is known for  $M$  wavelengths (or integration over  $M$  wavelength intervals  $\Delta\lambda$ ):

$$\underbrace{\begin{pmatrix} S(\lambda_1) \\ \vdots \\ S(\lambda_M) \end{pmatrix}}_S = \underbrace{\begin{pmatrix} R_1(\lambda_1) & \cdots & R_N(\lambda_1) \\ \vdots & \ddots & \vdots \\ R_1(\lambda_M) & \cdots & R_N(\lambda_M) \end{pmatrix}}_R \underbrace{\begin{pmatrix} A_1 \\ \vdots \\ A_N \end{pmatrix}}_A$$

To solve and obtain  $A_i$  for each pixel

# Linear spectral unmixing: principle

2 possibilities: **Emission:**

Single excitation wavelength, multi-spectral measurement (can be parallel)

**Excitation:**

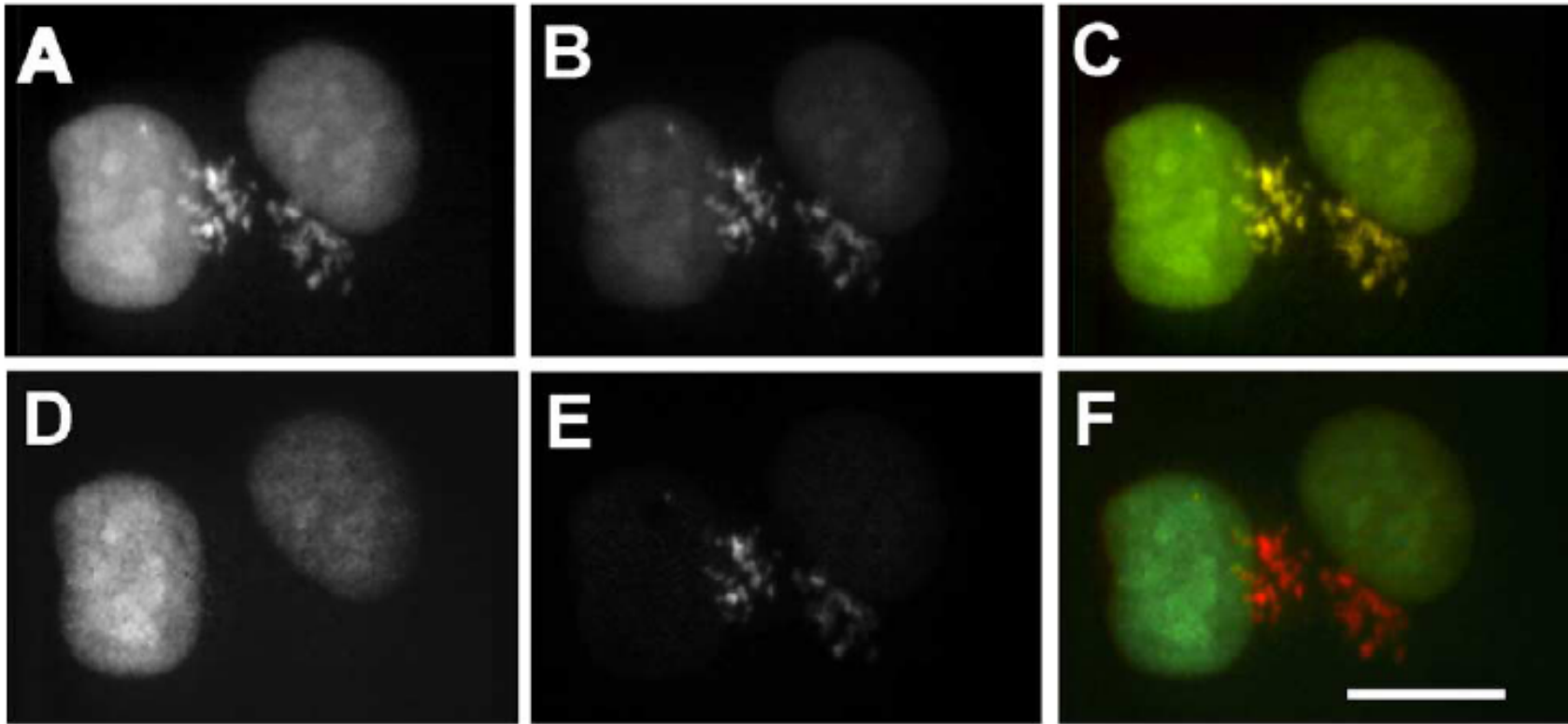
Multiple excitations wavelengths, one detection channel (can't be parallel)

**Hybrid:** Multiple excitation wavelengths, multiple detection channels (can be partially parallel)

## Criteria for Successful Linear Unmixing

- Number of channels should be at least equal to the number of fluorophores,  $M \geq N$
- All fluorophores present in the sample have to be considered for the unmixing (don't forget autofluorescence).  
*Note:* unmixing is not affected by taking into account fluorophore spectra in addition to the ones present in the sample.

# Spectral unmixing: GFP/YFP

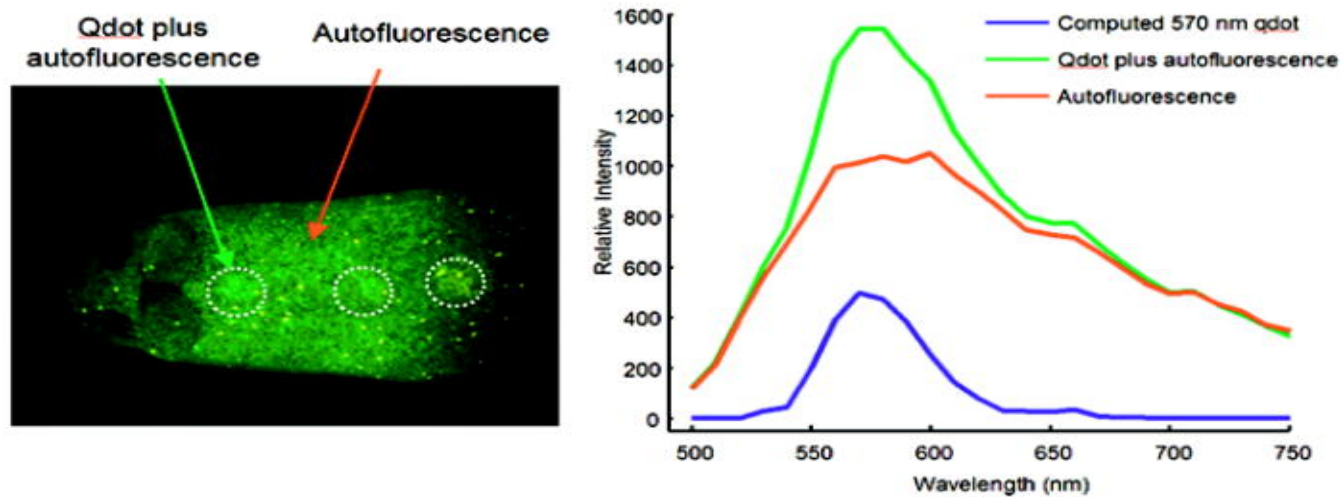


488 nm excitation, two channel detection (505–530nm, 530–565nm).

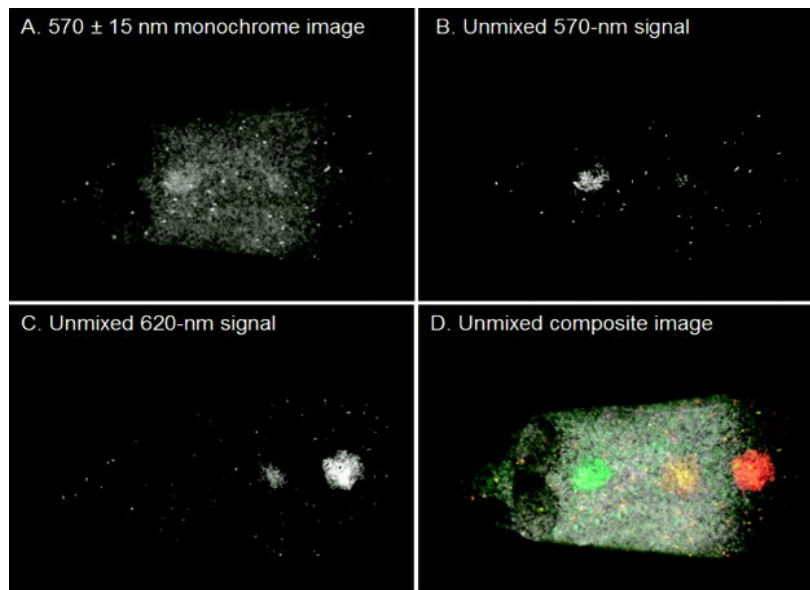
Histone-GFP (nucleus), YFP (Golgi)

From: Zimmermann T, Rietdorf J, Pepperkok R. Spectral imaging and its applications in live cell microscopy. *FEBS Lett* 2003;546:87–92.

# Spectral unmixing of autofluorescence



Red and green arrows indicate regions from which sample spectra were obtained.  
Blue = computed spectrum



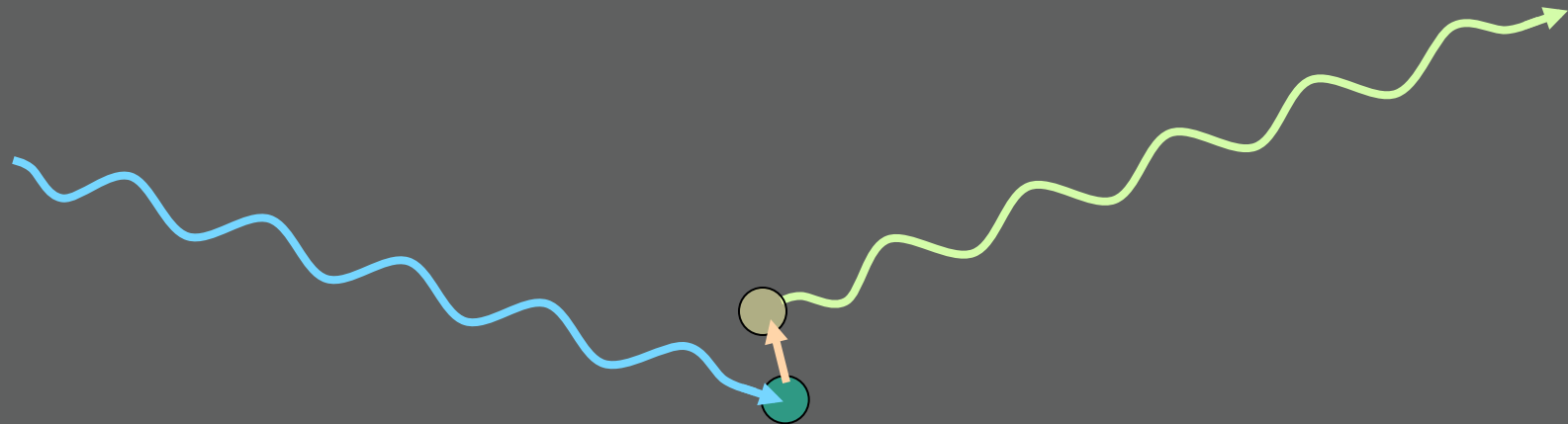
(a) Image obtained at the peak of one of the quantum dots.  
(b) Unmixed image of the 570-nm quantum dot.  
(c) Unmixed image of the 620-nm quantum dot.  
(d) Combined pseudocolor image of (b) (green), (c), and autofluorescence channel (in white).



FRET:

Resonance Energy Transfer (non-radiative)

The Good: FRET as a molecular yardstick



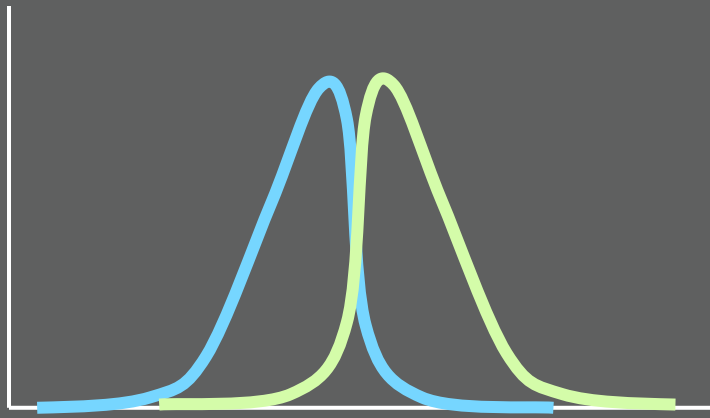
Transfer of energy from one dye to another

Depends on:

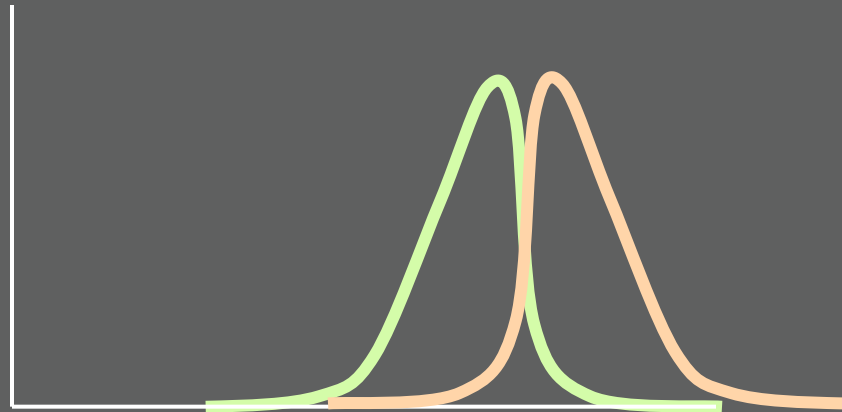
Spectral overlap

Distance

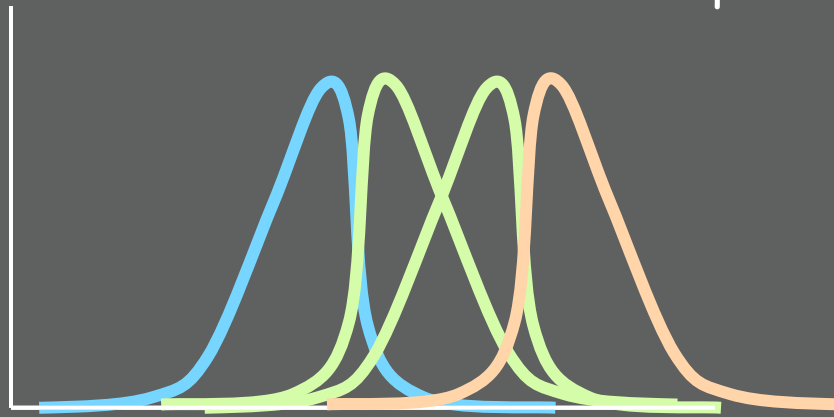
Alignment



donor



acceptor



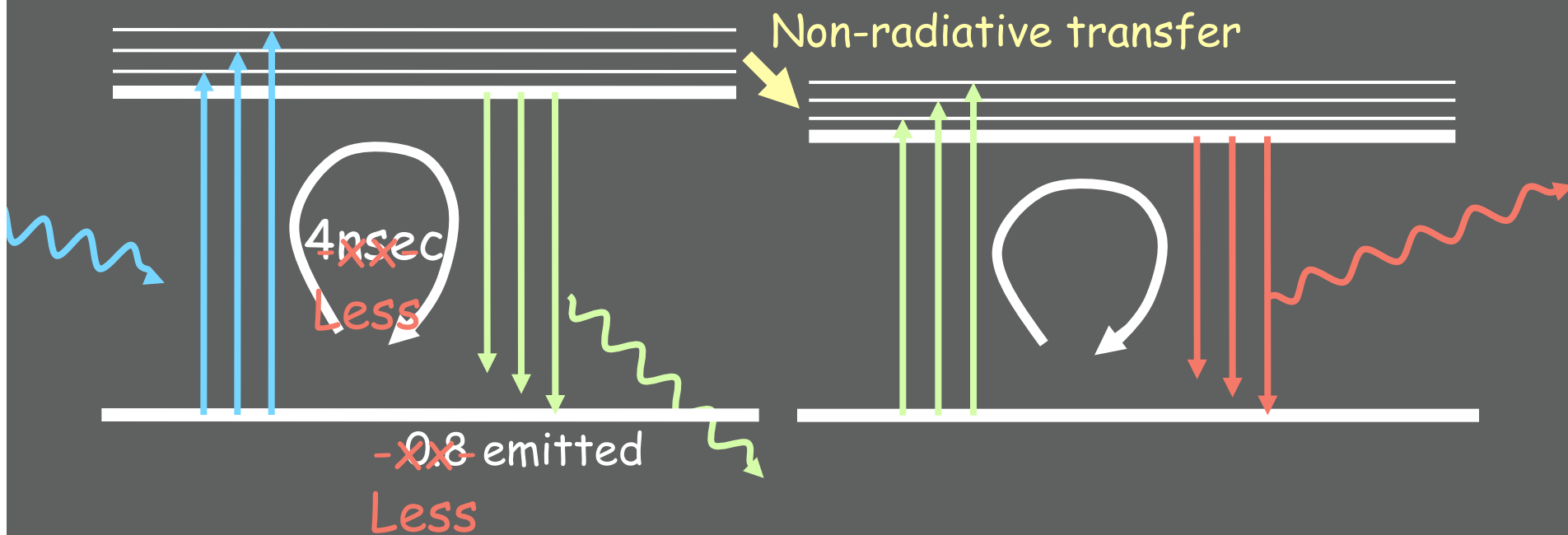
### FRET:

Optimize spectral overlap

Optimize  $\kappa^2$  -- alignment of dipoles

Minimize direct excitement of the acceptor  
(extra challenge for filter design)

# FRET Diagram



## The Förster Equations.

$$k_t = (R_0/r)^6 (1/\tau_d)$$

$$E = [1 + (r/R_0)^6]^{-1}$$

$$R_0 = [8.79 \times 10^{-25} J(\lambda) \kappa^2 Q_0 n^{-4}]^{-6}$$

$$J(\lambda) = \int f(\lambda) \varepsilon_A(\lambda) \lambda^4 d\lambda$$

$$f(\lambda) = F_D(\lambda) d\lambda / \int F_D(\lambda) d\lambda$$

$r$  is the center-to-center distance (in cm) between the donor and acceptor

$\tau_d$  is the fluorescence lifetime of the donor in the absence of FRET

$\kappa^2$  is the dipole-dipole orientation factor,

$Q_0$  is the quantum yield of the donor in the absence of the acceptor

$n$  is the refractive index of the intervening medium,

$F_D(\lambda)$  is the fluorescence emission intensity at a given wavelength  $\lambda$  (in cm)

$\varepsilon_A(\lambda)$  is the extinction coefficient of the acceptor (in  $\text{cm}^{-1} \text{M}^{-1}$ ).

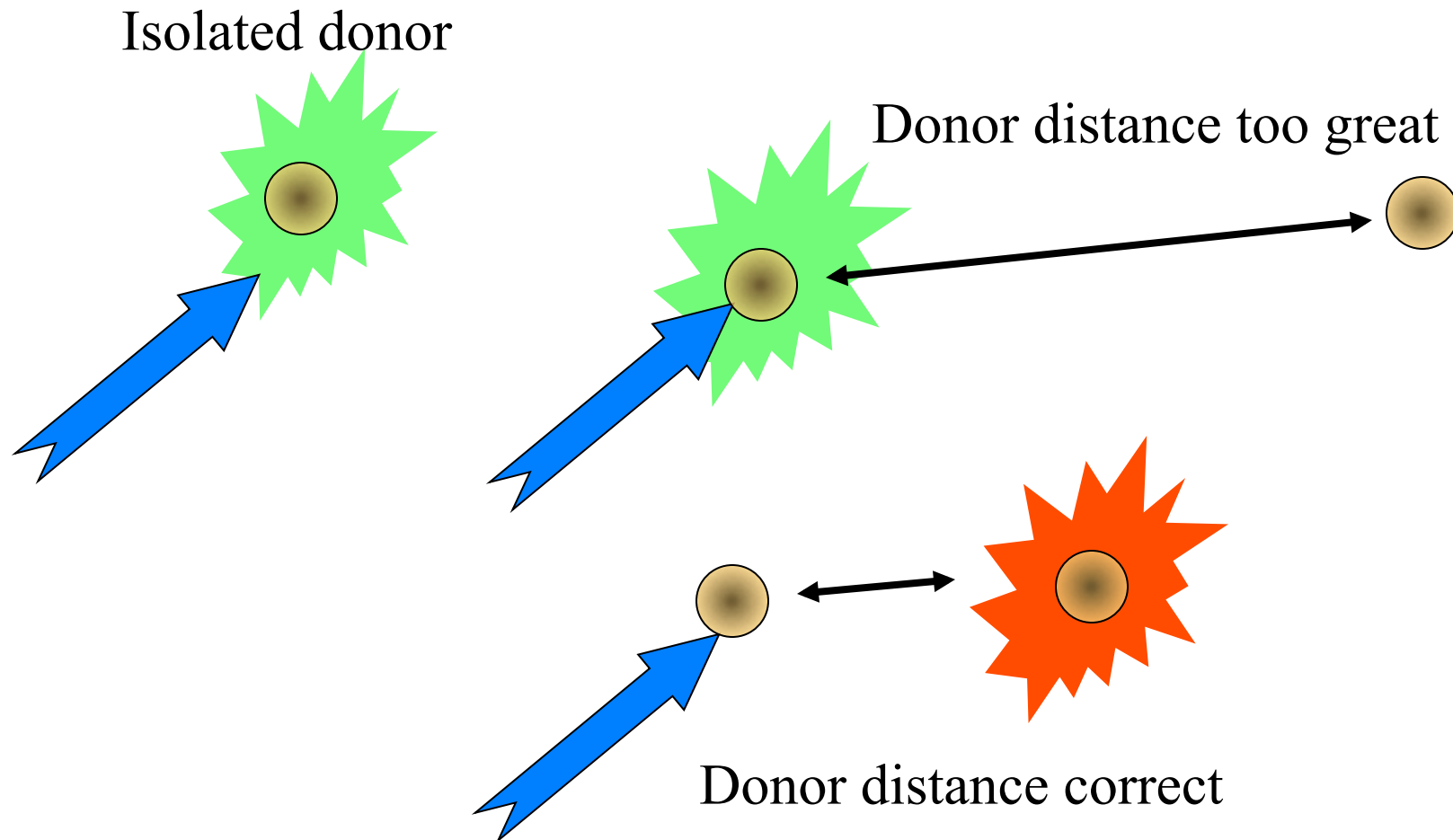
The orientation factor  $\kappa^2$  can vary between 0 and 4, but

typically  $\kappa^2 = 2/3$  for randomly oriented molecules (Stryer, 1978).

When  $r = R_0$ , the efficiency of FRET is 50%

(fluorescein-tetramethylrhodamine pair is 55 Å)

# More about FRET (Foster Resonance Energy Transfer)



**Effective between 10-100 Å only**

Emission and excitation spectrum must significantly overlap

Note: donor transfers non-radiatively to the acceptor

## Bi177 - Lecture 10

### “Quantitative“ Fluorescence

Fluorescence linearity (non-linearity)

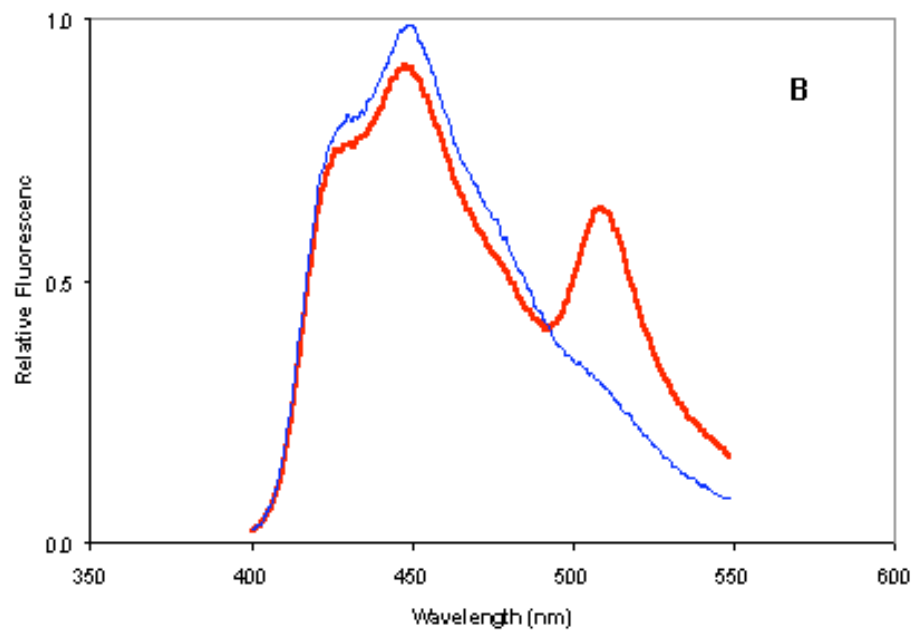
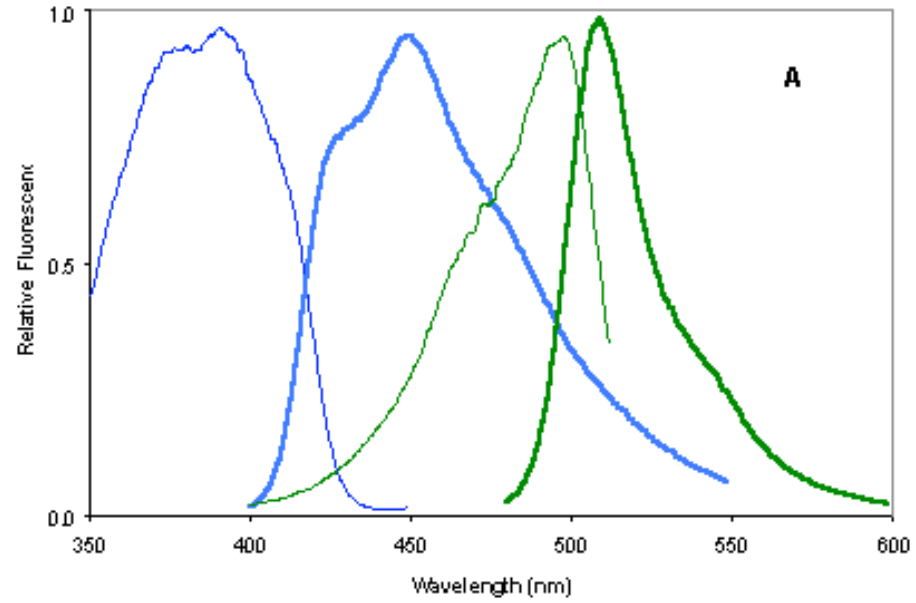
Dye, microscope, camera

Flat-fielding to linearize

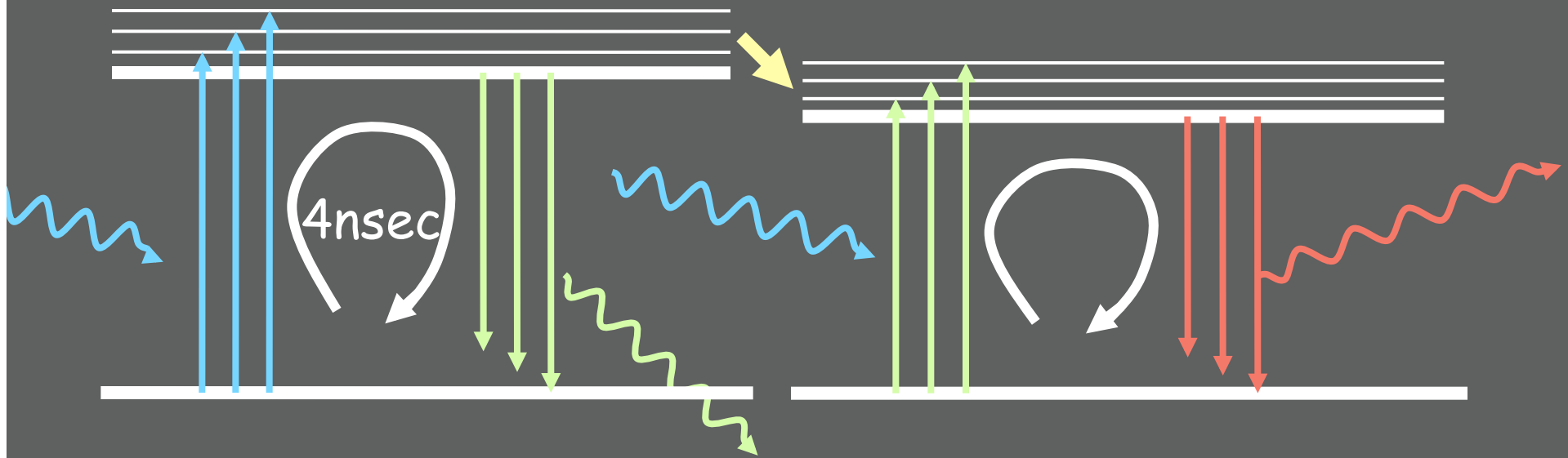
Quantitating the image

Multispectral imaging

FRET



## The realities strike



1. The acceptor excited directly by the exciting light
  - “FRET” signal with no exchange
  - Increased background
  - Decreases effective range for FRET assay



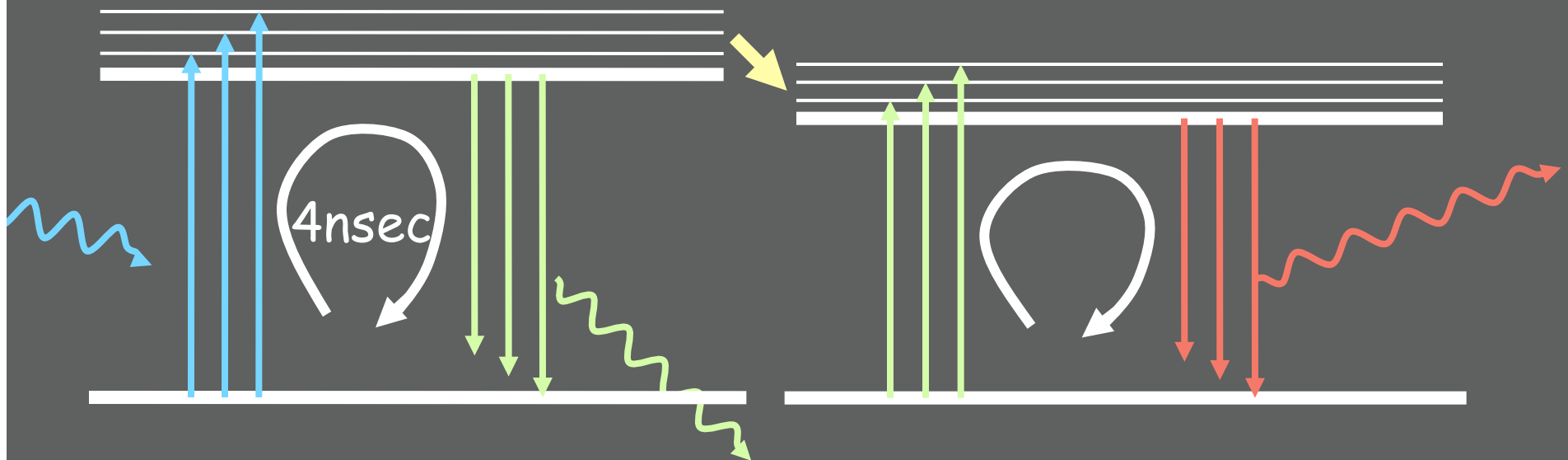
## The realities strike

2. Hard to really serve as a molecular yardstick\*

- Orientation seldom known  
assume  $\kappa^2 = 2/3$  (random assortment)
- Exchange depends on environment of dipoles
- Amount of FRET varies with the lifetime of the donor fluorochrome

\*  $r = R_0$ , the efficiency of FRET is 50%  
(fluorescein-tetramethylrhodamine pair is 55 Å)

Amount of FRET varies with the lifetime of the donor fluorochrome



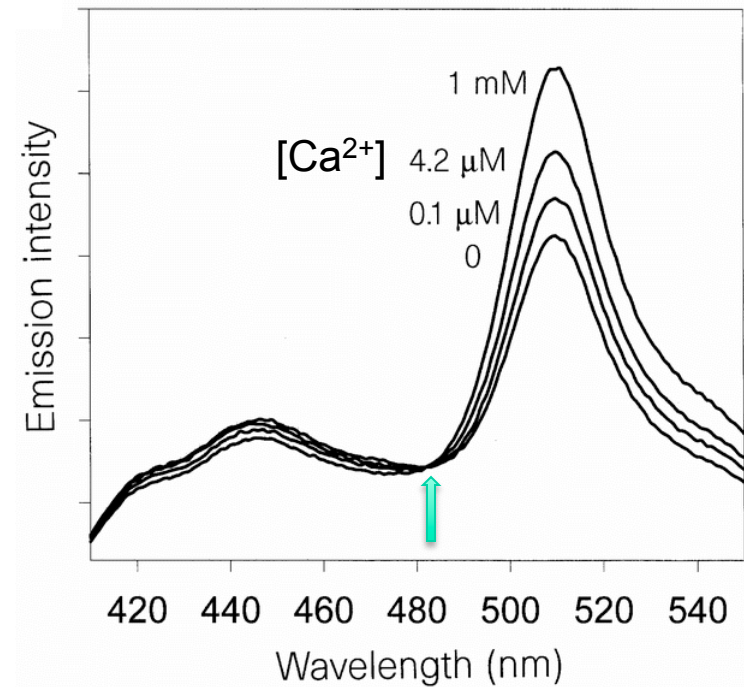
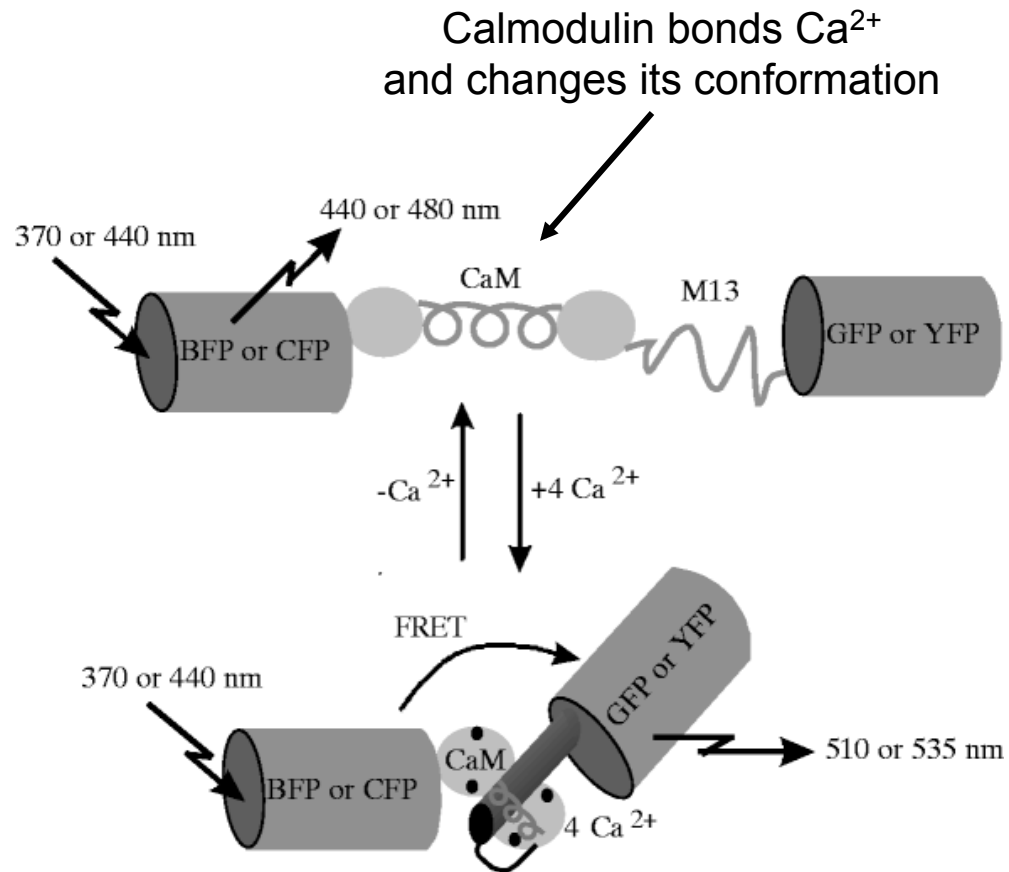
Longer lifetime of the donor gives longer time to permit the energy transfer (more for longer)  
Added Bonus: Allows lifetime detection to reject direct excitement of the acceptor (FRET=late)

# These drawbacks can all be used to make sensors

Change in FRET for changes in:

- Orientation  
cameleon dye for  $\text{Ca}^{++}$
- Local environment  
Phosphate near fluorochrome  
Membrane voltage (flash)
- Change in lifetime of donor  
Binding of molecule displacing water

# Cameleon: FRET-based and genetically-encoded calcium probe



Miyawaki et al, Nature, 1997

Cameleon family: calmodulin-based indicators of  $[\text{Ca}^{2+}]$  using FRET

isosbestic point

# Cameleon: FRET-based and genetically-encoded calcium probe

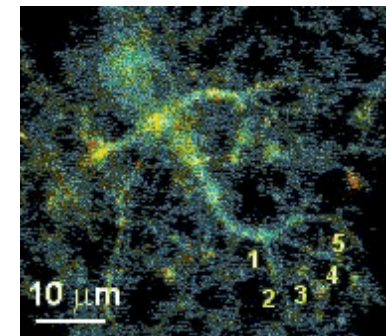
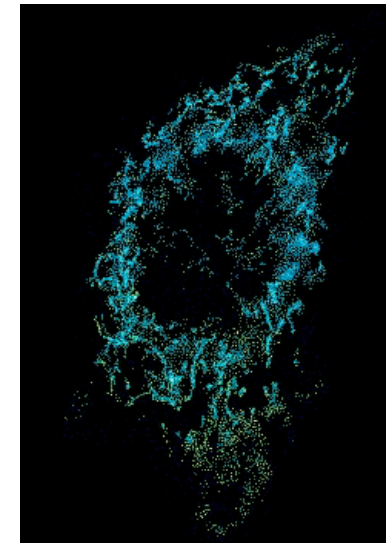
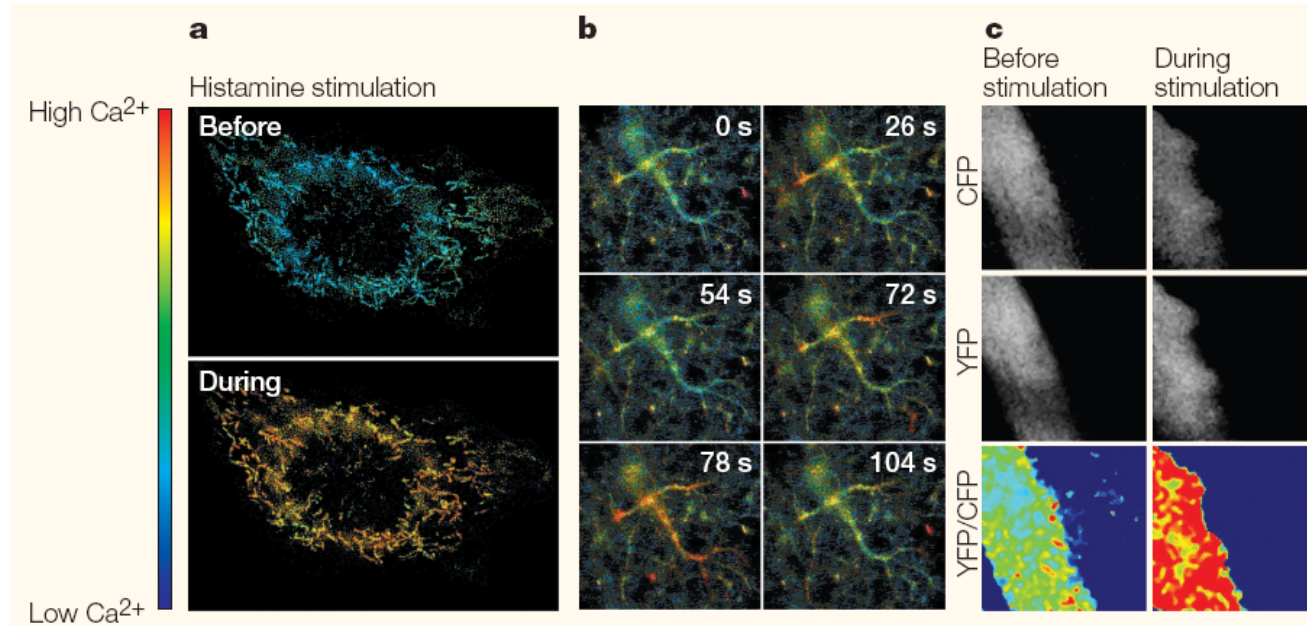


Figure 3 | **Examples of  $\text{Ca}^{2+}$ -concentration signalling in living cells.** **a** | Pseudo-colour-coded ratio-images obtained by conventional epifluorescence micrographs of a HeLa cell transfected with ratiometric pericam.  $\text{Ca}^{2+}$  concentrations are colour coded with a basal  $\text{Ca}^{2+}$  concentration in blue and a high  $\text{Ca}^{2+}$  concentration in yellow and red. Note the strong increase in mitochondrial  $\text{Ca}^{2+}$  concentration on histamine-induced release from the endoplasmic reticulum (see also [Online Video 1](#)). **b** | The pseudo-colour-coded ratio-images (as in FIG. 3a) of indo-1-loaded acute brain slices were obtained by confocal microscopy and show the  $\text{Ca}^{2+}$  waves in astrocytes that were induced by stimulation of the CA1 nerve fibres that contact the CA3 region of the hippocampus (known as the 'Schaffer collateral pathway') with an extracellular electrode, which results in the depolarization of the nerve terminals and the release of neurotransmitter. The panels show sequential frames of [Online Video 2](#). Note that the waves are sweeping from one process to another, traversing the whole cell. The numbers indicate the time after stimulation. **c** | Two-photon confocal micrographs of a muscle fibre from tibialis anterior muscle transfected with cytoplasmic cameleon in live mouse. The upper four panels show the yellow (YFP) and cyan fluorescence channel micrographs (CFP) from the cameleon probe that are responsible for the pseudo-colour-coded ratio-images (lower 2 panels) as in FIG. 3a. Note the increase in the intracellular  $\text{Ca}^{2+}$  concentration in the muscle on stimulation of the sciatic nerve.

Ratiometric dyes offer easiest quantitation

uncertainty from amount of dye loaded:

$\Delta F/F$  imaging can help

isosbestic point is best

Making a ratio dyes by standardizing with a second dye:

$F$  from indicator /  $F$  from standard

problem of different bleach rate

problem of different ISC to dark state

# Folding and bleaching of fluorescent proteins

## Example: properties of fluorescent protein variants

**Table 1 Properties of novel fluorescent protein variants**

Fluorescent protein	Excitation maximum (nm)	Emission maximum (nm)	Extinction coefficient per chain <sup>a</sup> ( $M^{-1}cm^{-1}$ )	Fluorescence quantum yield	Brightness of fully mature protein (% of DsRed)	pKa	$t_{0.5}$ for maturation at 37 °C	$t_{0.5}$ for bleach <sup>b</sup> , s
DsRed	558	583	75,000	0.79	100	4.7	~10 h	ND
T1	555	584	38,000	0.51	33	4.8	<1 h	ND
Dimer2	552	579	69,000	0.69	80	4.9	~2 h	ND
mRFP1	584	607	50,000	0.25	21	4.5	<1 h	6.2
mHoneydew	487/504	537/562	17,000	0.12	3	<4.0	ND	5.9
mBanana	540	553	6,000	0.70	7	6.7	1 h	1.4
mOrange	548	562	71,000	0.69	83	6.5	2.5 h	6.4
dTomato	554	581	69,000	0.69	80	4.7	1 h	64
tdTomato	554	581	138,000	0.69	160	4.7	1 h	70
mTangerine	568	585	38,000	0.30	19	5.7	ND	5.1
mStrawberry	574	596	90,000	0.29	44	<4.5	50 min	11
mCherry	587	610	72,000	0.22	27	<4.5	15 min	68

<sup>a</sup>Extinction coefficients were measured by the alkali denaturation method<sup>8,30</sup> and are believed to be more accurate than the previously reported values for DsRed, T1, dimer2 and mRFP1<sup>7</sup>.

<sup>b</sup>Time (s) to bleach to 50% emission intensity, at an illumination level that causes each molecule to emit 1,000 photons/s initially, that is, before any bleaching has occurred. See Methods for more details. For comparison, the value for EGFP is 115 s, assuming an extinction coefficient of  $56,000 M^{-1}cm^{-1}$  and quantum efficiency of 0.60 (ref. 30). ND, not determined.

Shaner et al, Nature Biotechnology, 2004

eGFP ~ 2h